



**IUCr Crystallographic Computing School**

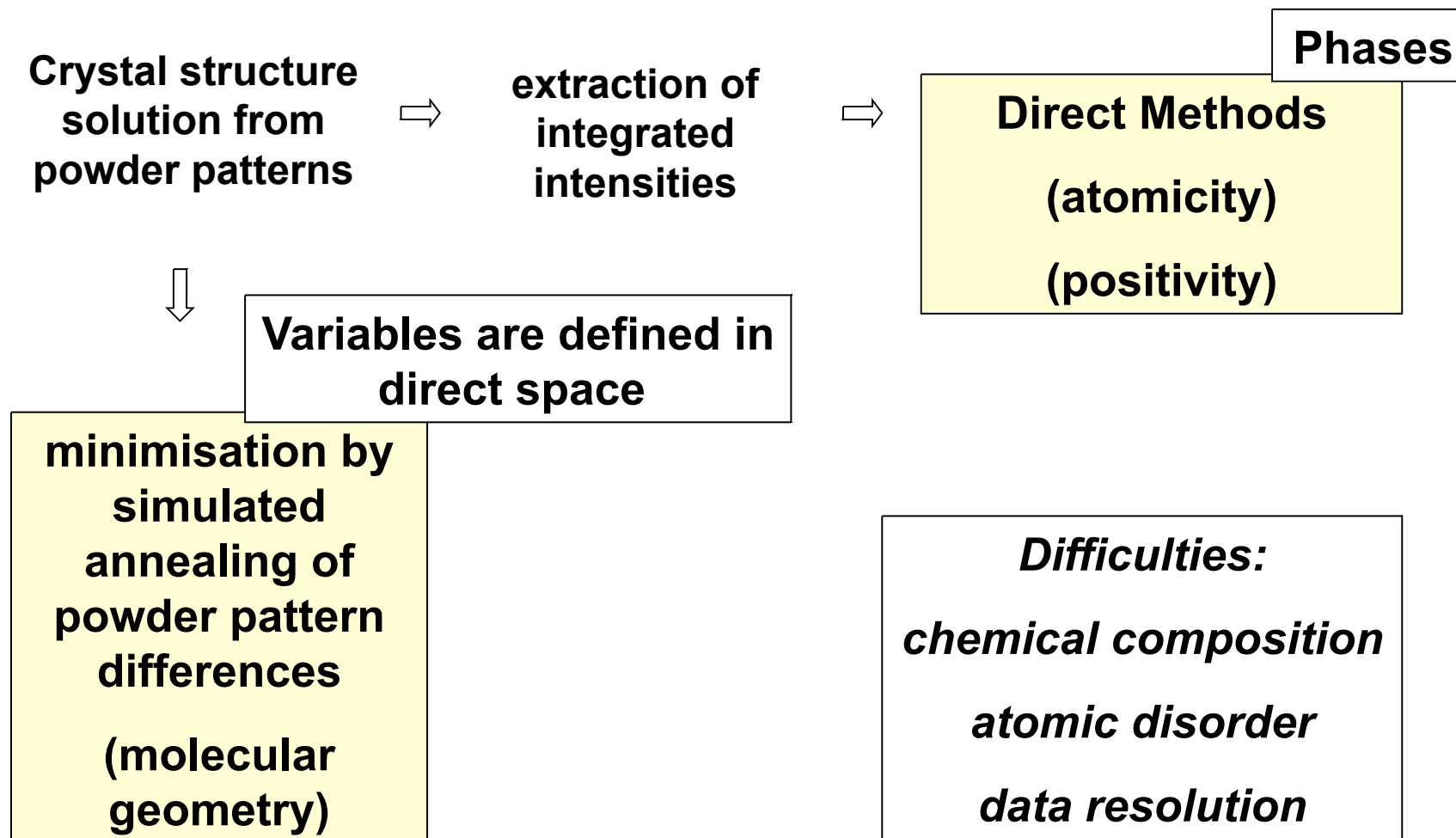
**16-21st August 2011 Oviedo (Spain)**

# **Direct Methods Algorithms in Powder Diffraction**

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# Solving structures from powder data



# First remarkable applications of conventional DM to powder data

- 1/ **Rudolf, Saldariaga-Molina, Clearfield**  
*J.Phys.Chem.* (1986) **90**, 6122-6125.  
Synthetic aluminophosphate, structure type: ATT,  $P2_12_12_1$ , CuK $\alpha$
  
- 2/ **McCusker (1988)**  
*J.Appl.Cryst.* (1988) **21**, 305-310.  
Sigma-2, a silica clathrasil, structure type: SGT,  $I4_1/amd$ ,  $\lambda=1.55\text{\AA}$
  
- 3/ **Cernik, Cheetham, Prout, Watkin, Wilkinson, Willis**  
*J.Appl.Cryst.* (1991) **24**, 222-226.  
Cimetidine ( $C_{10}H_{16}N_6S$ ),  $P2_1/c$ ,  $\lambda=1.46\text{\AA}$
  
- 4/ **Oberhagemann, Bayat, Marler, Gies, Rius**  
*Angew.Chem.Int.Ed.Engl.*(1996) **35**, 2869.  
RUB-15, a layer silicate solved at  $2\text{\AA}$  resolution,  $Iba2$ , CuK $\alpha_1$

# Intensities improvement

Intensities are normally extracted either using the **Pawley (1981)** or the **LeBail (1988)** method. Peak overlap can be treated by equi-distributing the multiplet intensity. Other more sophisticated methods are (if applicable):

**Squared Patterson function:** Estermann, McCusker, Baerlocher (1992) J.Appl.Cryst. 25, 539-543

**Anisotropic expansion:** Shankland, David, Sivia (1997) J.Mater.Chem. 7, 569-572

**Texture:** Wessels, Baerlocher, McCusker (1999) Science 284, 477-479

**Preferred orientation** (statistical check): Altomare, Cascarano, Giacovazzo, Gugliardi (1994) J.Appl.Cryst. 27, 1045-1050.

## Some Relevant DM Algorithms for Powder Diffraction (1)

- (1995) Rius, Sañé, Miravittles, Gies, Marler, Oberhagemann *Acta Cryst A* **51** 840-845  
*SF applied to intensity data at 2Å resolution*
- (1997) Grosse-Kunstleve, McCusker, Baerlocher *Acta Cryst A* **30** 985-995  
*FOCUS algorithm incorporating framework information*
- (1997) Brenner, McCusker, Baerlocher *J. Appl. Cryst.* **30** 1167-1172  
*Use of envelopes to aid phase determination*
- (1999) Rius, Miravittles, Gies, Amigó *J. Appl. Cryst.* **32** 89-87  
*Proof that SF can be applied to data with systematic overlap*
- (2000) Rius, Torrelles, Miravittles, Ochando, Reventós, Amigó *J. Appl. Cryst.* **33** 1208-1211  
*SF applied to data with accidental overlap (Overlapped E's are updated)*
- (2002) Altomare, Cuocci, Giacovazzo, Gugliardi, Moliterni, Rizzi *J. Appl. Cryst.* **35** 182-184  
*DM + Fourier recycling improvements*
- (2005) Rius-Palleiro, Peral, Margiolaki, Torrelles *J. Appl. Cryst.* **38** 906-911  
*'Envelope' determination from isomorphous-replacement to fix some phases*

## Some Relevant DM Algorithms for Powder Diffraction (2)

- (2006) Wu,Leineweber,Spence,O'Keefe *Nature* **5** 647-652  
*CF and E's modification*
- (2007) Baerlocher,McCusker,Palatinus *Z.Kristallogr.* **222** 47-53  
*CF and histogram matching*
- (2007) Rius,Frontera *J.Appl.Cryst.* **40** 1035-1038  
*SF (in Fourier space) with E's treatment*
- (2007) Baerlocher,Gramm,Massüger,McCusker,He,Hovmöller,Zou *Science* **315** 1113-16  
*CF and electron microscopy information*
- (2008) Altomare,Caliandro,Cuocci,Giacovazzo,Moliterni et al. *J.Appl.Cryst.* **41** 56-61  
*DM and simulated annealing*
- (2008) Altomare,Cuocci,Giacovazzo,Kamel,Moliterni,Rizzi *Acta Cryst.* **A64** 326-336  
*DM and minimally resolution biased electron-density maps*
- (2011) Rius *Acta Cryst* **A67** 63-67  
*Patterson SF (in Fourier space) with individual & overlapped I as observed data*

*DM=conventional direct methods in reciprocal space*

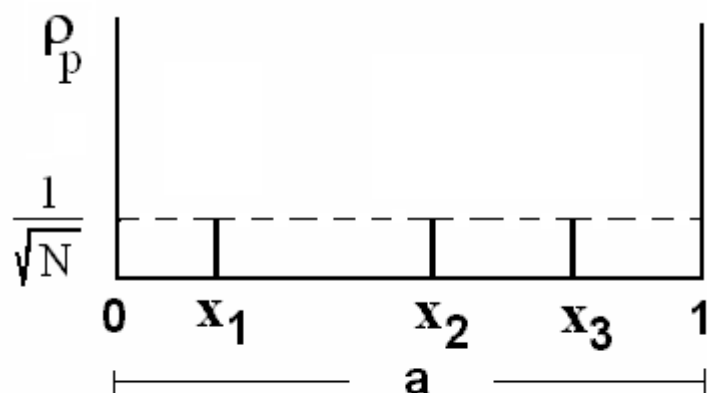
*SF= direct methods sum function*

*CF= charge-flipping*

# The normalised structure factors

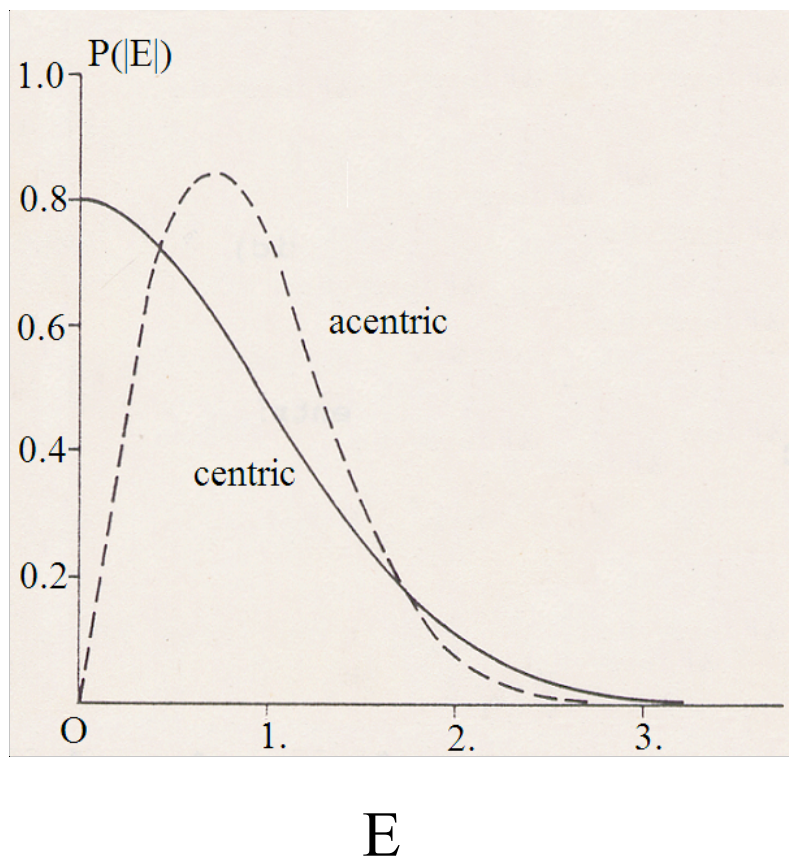
$$E^2 = \frac{F^2}{\sum_j f_j^2}$$

Form factor fall-off and thermal vibration decay are removed.  
For a crystal structure with  $N$  equal atoms in the unit cell:



$$\mathbf{E}_H = \frac{1}{\sqrt{N}} \cdot \sum_j e^{i2\pi Hx_j} = E_H \cdot e^{i\phi_H}$$

# The distribution of E's



Wilson (1949) *Acta Cryst.* **2**, 318

$$P_1(E) = \frac{2}{\pi} \cdot E \cdot \exp(-E^2)$$

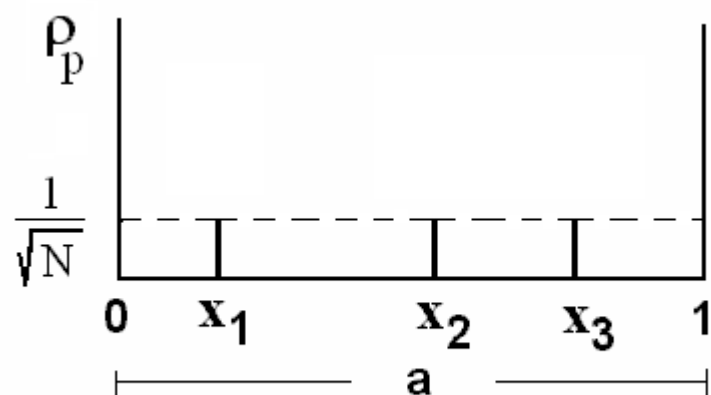
$P_1(E)$  is independent of the structure complexity and holds for any random distribution of atoms in the unit cell. From  $P_1(E)$ , the theoretical  $\langle E^2 \rangle$  and  $\langle E \rangle$  values can be derived.

	<b>acentric</b>
$\langle E^2 \rangle$	<b>1.00</b>
$\langle E \rangle$	<b>0.886</b>

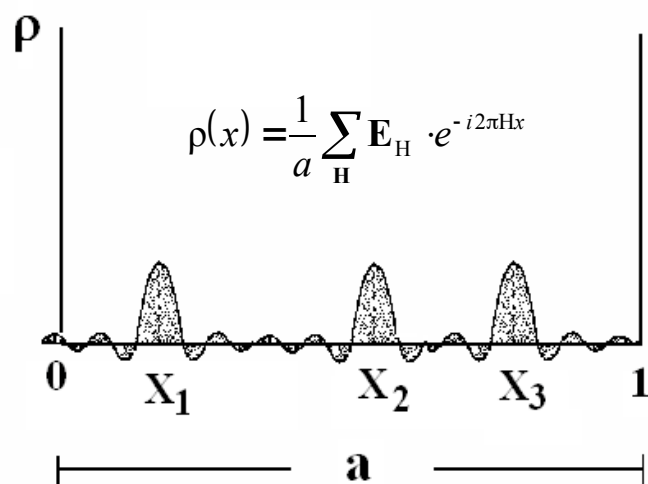
(adapted from D. Viterbo, *Direct methods of Solving Crystal Structures* pp.58, Ed. By H.Schenk, Plenum Press, New York, 1991)



# The electron density function



$$\Rightarrow \mathbf{E}_H = \frac{1}{\sqrt{N}} \cdot \sum_j e^{i2\pi Hx_j} = E_H \cdot e^{i\phi_H}$$



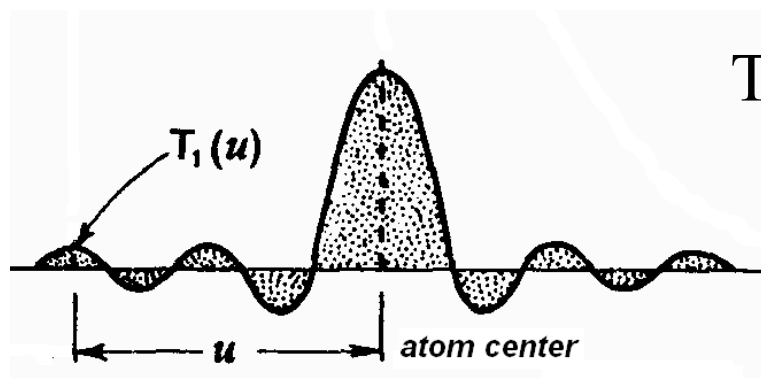
$$\leftarrow \rho(\mathbf{r}) = \frac{1}{V} \sum_H \mathbf{E}_H \cdot e^{-i2\pi H\mathbf{r}}$$

(Limited number of Fourier terms)

**ATOMIC RESOLUTION !**

# Data resolution and spreading function

Calculation of  $\rho$  with a finite number of Fourier terms (with  $E$ 's) gives no point atoms. The density distribution is spread.



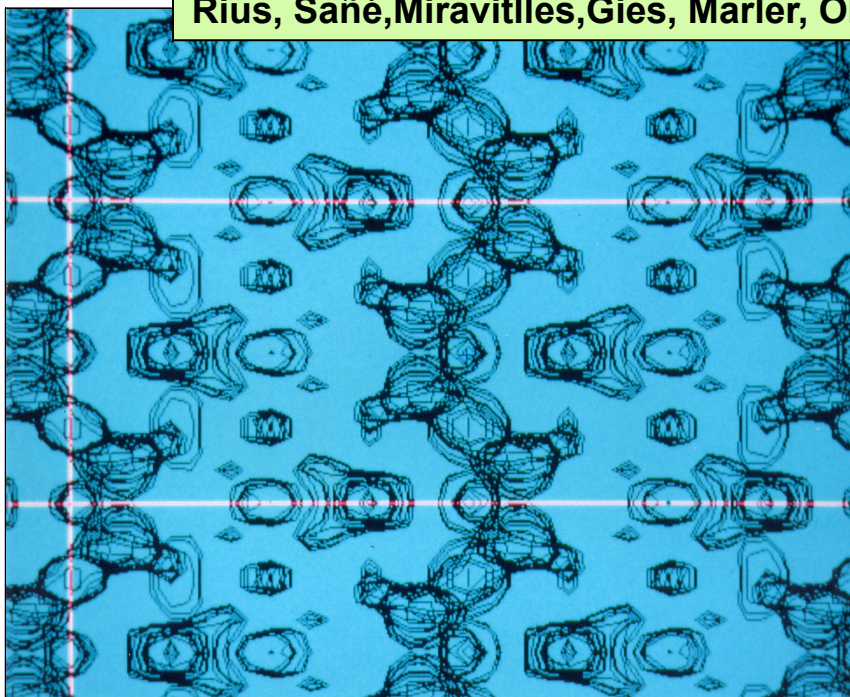
$$T_1(u) = 2 \cdot r_{max}^* \cdot \frac{\sin(2\pi r_{max}^* u)}{2\pi r_{max}^* u}$$

(From Lipson & Cochran, 1966)

**3D case:** 1st zero of  $T_3(u)$  at  $0.72/r_{max}^*$

# Image of the layer silicate RUB-15 at 2 Å resolution

Rius, Sañé, Miravittles, Gies, Marler, Oberhagemann Acta Cryst. (1995) A51, 840-845.



## Application of the SUMF-TF

- 76 independent intensities up to  $2\theta_{\max} = 41.5^\circ$  for Cu  $K\alpha_1$  (almost complete data set)

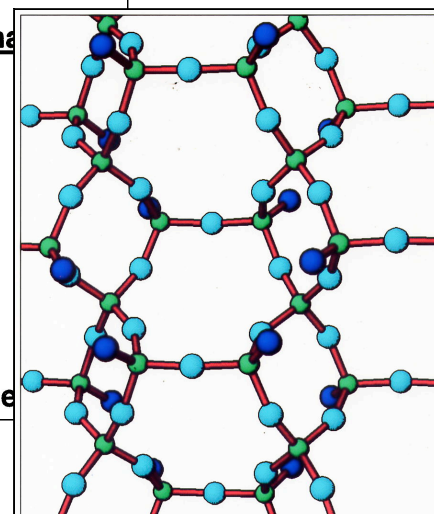


2 Angstroms resolution

- $S_D(\text{Si-Si}) \cong 3.1 \text{ \AA} \Rightarrow d_{\min} \cong 2.15 \text{ \AA}$

## Parameters introduced in the phase refinement:

- 20 strongest E's  $\Rightarrow$  65 triplets
- 16 weakest E's  $\Rightarrow$  98 triplets
- 100 sets refined
- 13 cycles per set
- selection of the solution with the best fit

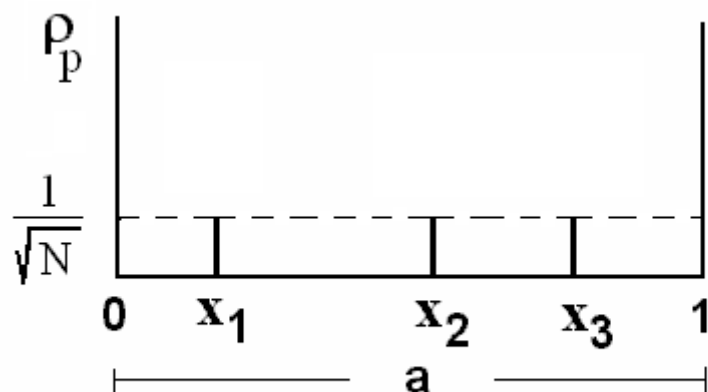


(100) projection of the silicate layer of RUB-15

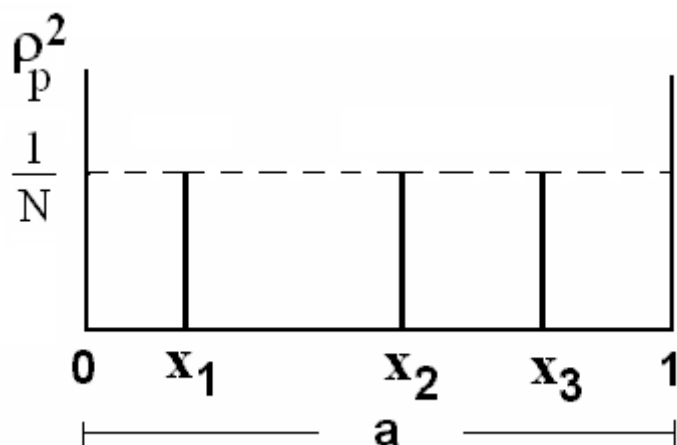
$$a = 27.911 \quad b = 8.408 \quad c = 11.516 \text{ \AA}$$

*Iba2 (Ibam)*

# The s.f. of the squared structure



$$\mathbf{E}_{\mathbf{H}} = \frac{1}{\sqrt{N}} \cdot \sum_j e^{i2\pi\mathbf{H}x_j} = \mathbf{E}_{\mathbf{H}} \cdot e^{i\phi_{\mathbf{H}}}$$



$$\mathbf{G}_{\mathbf{H}} = \frac{1}{N} \cdot \sum_j e^{i2\pi\mathbf{H}x_j} = \mathbf{G}_{\mathbf{H}} \cdot e^{i\psi_{\mathbf{H}}}$$

$$\mathbf{G}_{\mathbf{H}} = \frac{\mathbf{E}_{\mathbf{H}}}{\sqrt{N}}$$

$$\phi_{\mathbf{H}} \approx \psi_{\mathbf{H}}$$

For large H !



# The DM origin-free modulus sum function

$G$  is expressed in terms the  $\Phi$  set of phases.

For any set of  $G(\Phi)$  fulfilling the atomicity condition, then  $\langle G(\Phi) \rangle \approx \langle G(\Phi_{\text{true}}) \rangle$  so that

$$R_M(\Phi) = \sum_{\mathbf{H}} \left\{ (G_{\mathbf{H}} - \langle G \rangle) - [G_{\mathbf{H}}(\Phi) - \langle G(\Phi) \rangle] \right\}^2 = \text{min!}$$

is equivalent to maximising  $S_M$

$$S_M(\Phi) = \frac{2}{\sqrt{N}} \sum_{\mathbf{H}} (E_{\mathbf{H}} - \langle E \rangle) \cdot G_{\mathbf{H}}(\Phi) = \text{max!}$$

## Physical meaning of $S_M$ (I)

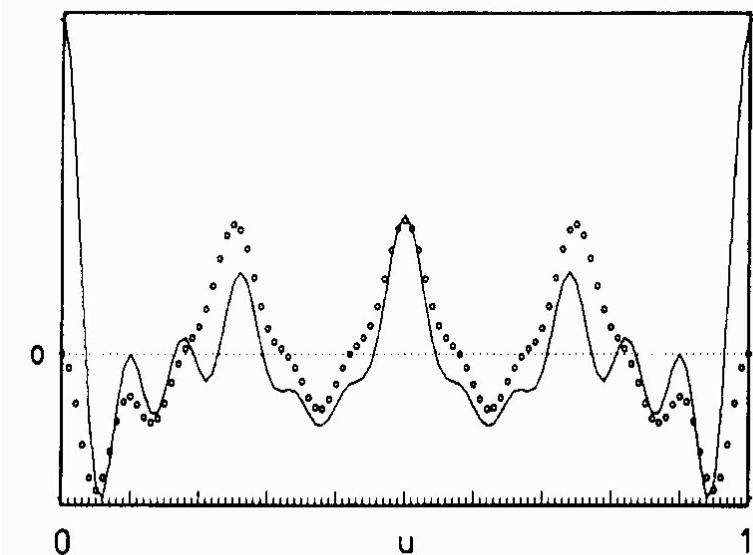
$$S_M(\Phi) = \frac{2}{\sqrt{N}} \sum_{\mathbf{H}} (E_{\mathbf{H}} - \langle E \rangle) \cdot G_{-\mathbf{H}}(\Phi)$$

is the reciprocal space form for

$$S_M(\Phi) \propto \int_V P'_M(\mathbf{u}) \cdot P_M(\mathbf{u}, \Phi) \cdot d\mathbf{u}$$

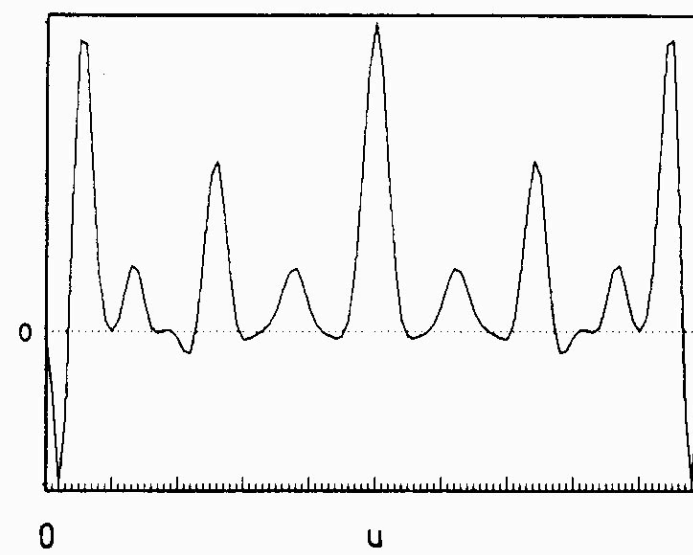
# Physical meaning of $S_M$ (II)

$$S_M(\Phi) \propto \int_V P'_M(\mathbf{u}) \cdot P_M(\mathbf{u}, \Phi) \cdot d\mathbf{u}$$



(a)

$P'_M(u)$  (dots) and  $P_M(u, \Phi)$  (line)



(b)

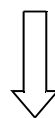
$P'_M(u) \cdot P_M(u, \Phi)$

## $\mathbf{G}_H$ in terms of $\Phi = \{\dots, \varphi_h, \dots\}$

Direct space:  $\rho^2(\Phi) = \rho(\Phi) \cdot \rho(\Phi)$  (if atomicity holds)

Reciprocal space:

$$\begin{aligned} \mathbf{G}_{-H}(\Phi) &= \mathbf{G}_{-H}(\Phi) \cdot e^{i\psi_{-H}(\Phi)} \\ &= \frac{1}{V} \sum_{\mathbf{h}} E_{-h} E_{H-h} e^{i(\phi_{-h} + \phi_{h-H})} \end{aligned}$$



$$\mathbf{G}_{-H}(\Phi) = \frac{1}{V} \sum_{\mathbf{h}} E_{-h} E_{H-h} e^{i(\phi_{-h} + \phi_{h-H} + \psi_H)}$$



## $S_M$ rearrangement

Expression  $S_M = (2/\sqrt{N}) \sum_H (E_H - \langle E \rangle) G_{-H}(\Phi)$  can be rearranged in the form

$$S_M = \frac{2}{\sqrt{N}} \sum_h E_{-h} e^{i\phi_{-h}} \left\{ \frac{1}{V} \sum_H (E_H - \langle E \rangle) \cdot E_{h-H} e^{i(\psi_H + \phi_{h-H})} \right\} \cong \cong \cong$$



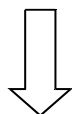
$\{\dots\} =$  Fourier coefficient of  $\delta_M' = \delta_M \cdot \rho$

$$\rho = FT^{-1} \{ E_H \cdot \exp i\phi_H \}$$

$$\delta_M = FT^{-1} \{ (E_H - \langle E \rangle) \cdot \exp i\psi_H \}$$

# How to maximise $S_M$

$$S_M = \frac{2}{\sqrt{N}} \sum_{\mathbf{h}} E_{-\mathbf{h}} e^{i\phi_{-\mathbf{h}}} \left\{ \frac{1}{V} \sum_{\mathbf{H}} (E_{\mathbf{H}} - \langle E \rangle) \cdot E_{\mathbf{h}-\mathbf{H}} e^{i(\psi_{\mathbf{H}} + \phi_{\mathbf{h}-\mathbf{H}})} \right\}$$



## Sequential mode

( $S_M$ -TF refinement using phase relationships, explicitly)

$$E_{-\mathbf{h}} (E_{\mathbf{H}} - \langle E \rangle) E_{\mathbf{h}-\mathbf{H}} \exp i(\phi_{-\mathbf{h}} + \psi_{\mathbf{H}} + \phi_{\mathbf{h}-\mathbf{H}})$$

Rius (1993) *Acta Cryst A* **49**, 406-409

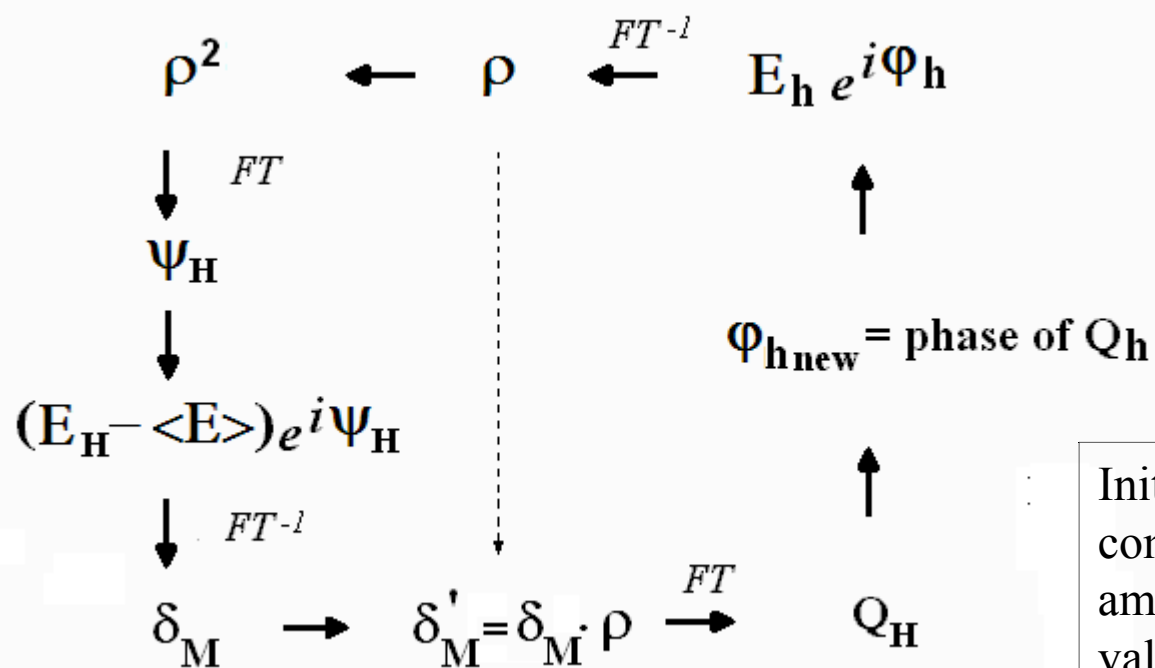


## Parallel mode

S-FFT algorithm

Rius et al. (2007) *Acta Cryst A* **63**, 131-134

# The $S_M$ -FFT algorithm



Initial phase values are combined with experimental amplitudes to give initial  $\rho$  values (upper right corner). New structure factor estimates  $Q$  are obtained by Fourier transforming  $\delta'_M$ .

# Patterson-function direct methods

$$S_M(\Phi) \propto \int_V P_M'(\mathbf{u}) \cdot P_M(\mathbf{u}, \Phi) d\mathbf{u}$$

Patterson-function DM are based on the existing proportionality between non-origin peaks of modulus and Patterson functions:

$$S_P(\Phi) \propto \int_V P'(\mathbf{u}) \cdot P_M(\mathbf{u}, \Phi) d\mathbf{u}$$

$$S_P(\Phi) = (2/N) \sum_{\mathbf{H}} (I_{\mathbf{H}} - \langle I \rangle) \cdot G_{-\mathbf{H}}(\Phi)$$

## Rearrangement of $S_P$

In parallel to  $S_M$ ,  $S_P$  can be rearranged to

$$S_P = \frac{2}{N} \sum_{\mathbf{h}} E_{-\mathbf{h}} e^{i\phi_{-\mathbf{h}}} \left\{ \frac{1}{V} \sum_{\mathbf{H}} (I_{\mathbf{H}} - \langle I \rangle) \cdot E_{\mathbf{h}-\mathbf{H}} e^{i(\psi_{\mathbf{H}} + \phi_{\mathbf{h}-\mathbf{H}})} \right\}$$

↓

$\{...\}$  is the Fourier coefficient of  $\delta_p = \rho \cdot \delta_p$

$$\rho = FT^{-1} \{ w_{\mathbf{H}} \cdot E_{\mathbf{H}} \cdot \exp i\phi_{\mathbf{H}} \}$$

$$\delta_p = FT^{-1} \{ (I_{\mathbf{H}} - \langle I \rangle) \cdot \exp i\psi_{\mathbf{H}} \}$$

# Powder diffraction intensities

$D_i$  ,  $n_i$  = global intensity and number of contributing reflections for multiplet  $i$

## Intensity of H reflection:

$$I_H = D_i/n_i$$

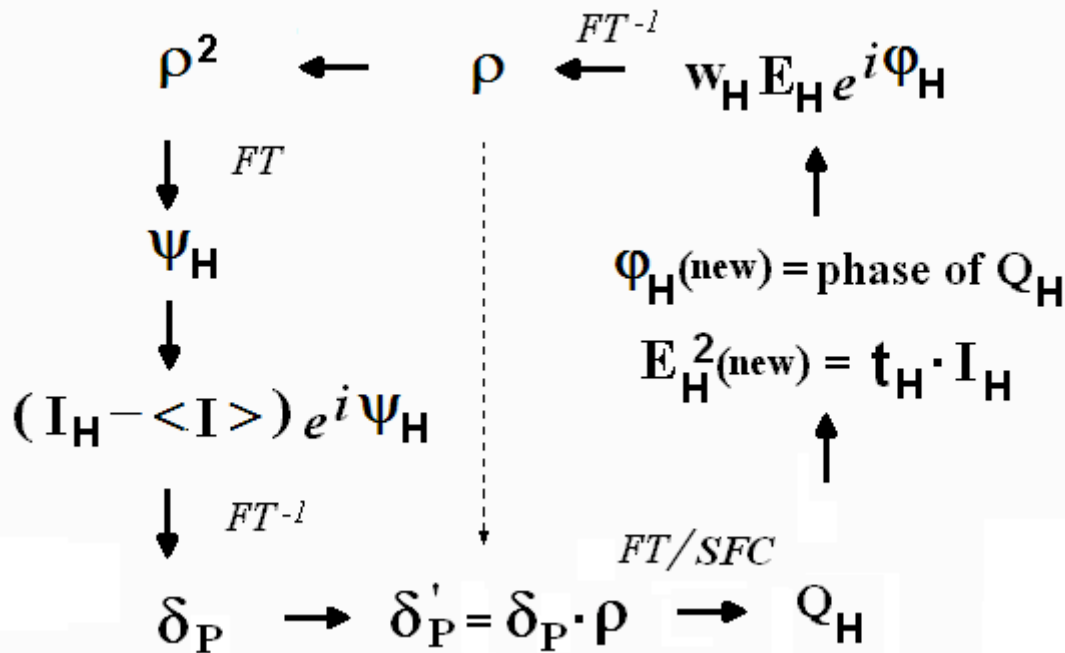
(all reflections of one multiplet have same I)

## Average intensity:

$$\langle I \rangle = (\sum_H I_H)/N_H = (\sum_i D_i)/N_H$$

Notice that  $\langle I \rangle = \langle E^2 \rangle$

# $S_p$ -FFT algorithm for Patterson-function DM with powder data



Initial phase values are combined with experimental and extrapolated amplitudes to give initial  $\rho$  values (upper right corner). The measured multiplet intensities are introduced via the  $(I_H - \langle I \rangle)$  coefficients. New structure factor estimates are obtained either by Fourier transforming  $\delta_p'$  or directly from the  $N$  top-ranked Fourier peaks (*SFC*) of  $\delta_p'$ . For overlapped reflections,  $E_H^2$  values are updated every cycle while keeping the global intensity of each multiplet constant.

$$E_H^2(\text{new}) = \left( \frac{n_i Q_H^2}{\sum_k j_{k(i)} Q_{k(i)}^2} \right) I_H = t_H I_H$$



## INORGANIC V.S. ORGANIC COMPOUNDS IN POWDER DIFFRACTION

**Reasons for the success in solving crystal structures from inorganic compounds (IC) compared to molecular ones:**

- 1) IC tend to have smaller unit cells or higher metrics (less accidental peak overlap);
- 2) IC possess longer bond distances (less data resolution requirements);
- 3) IC contain stronger scatterers with higher contrast (smaller effective number of atoms);
- 4) IC are more stable (consistency of the measured data set over the whole 2-theta range).



# Aerinite blue

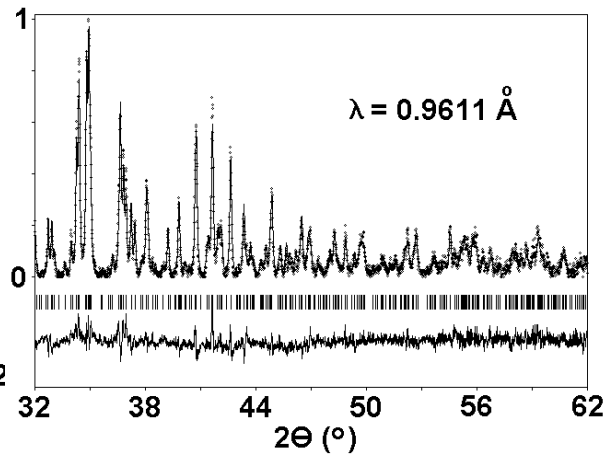
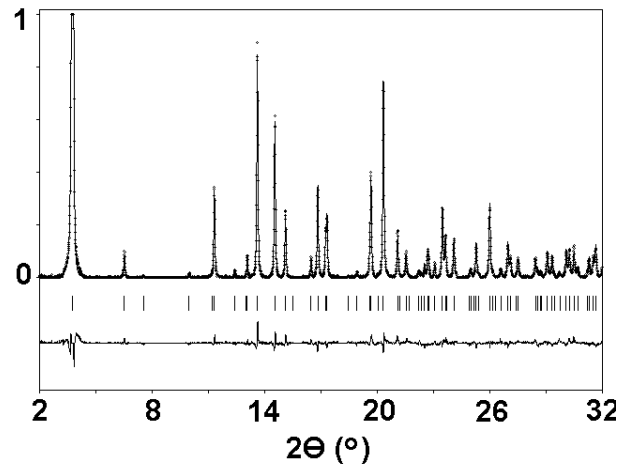
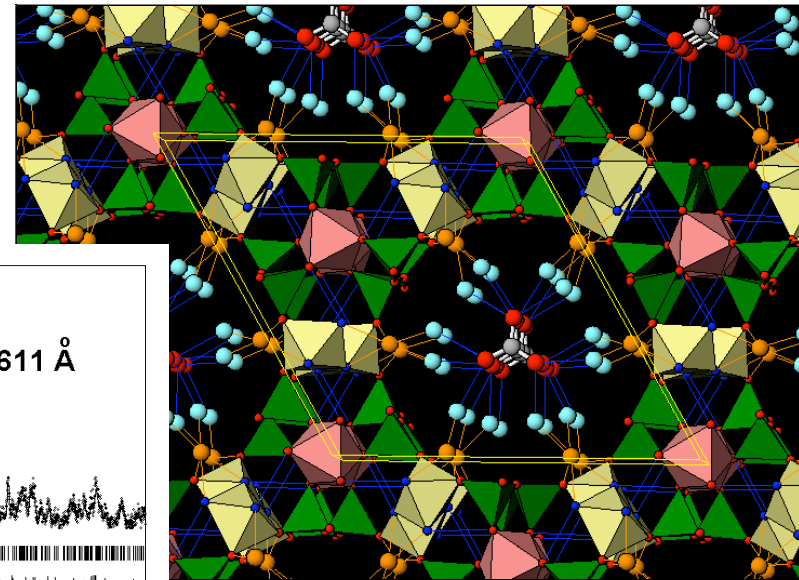
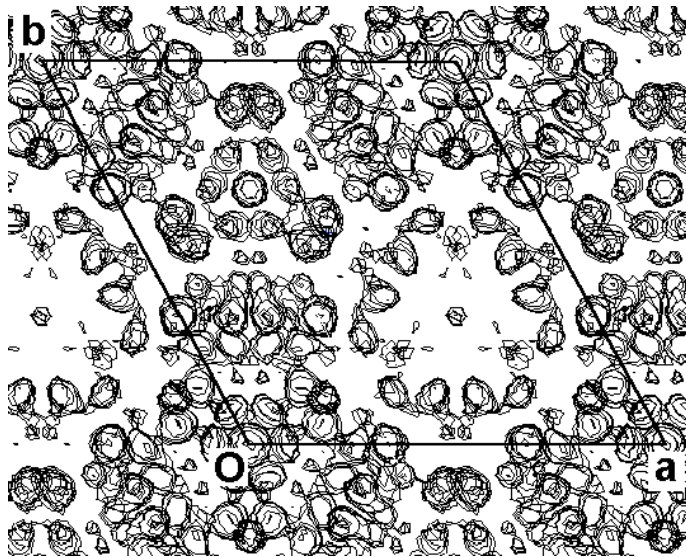
$a = 16.882$   $c = 5.225 \text{ \AA}$ ,  $P3c1$

250 integrated intensities mostly affected by systematic overlap

(LURE DW22, capillar 1mm)

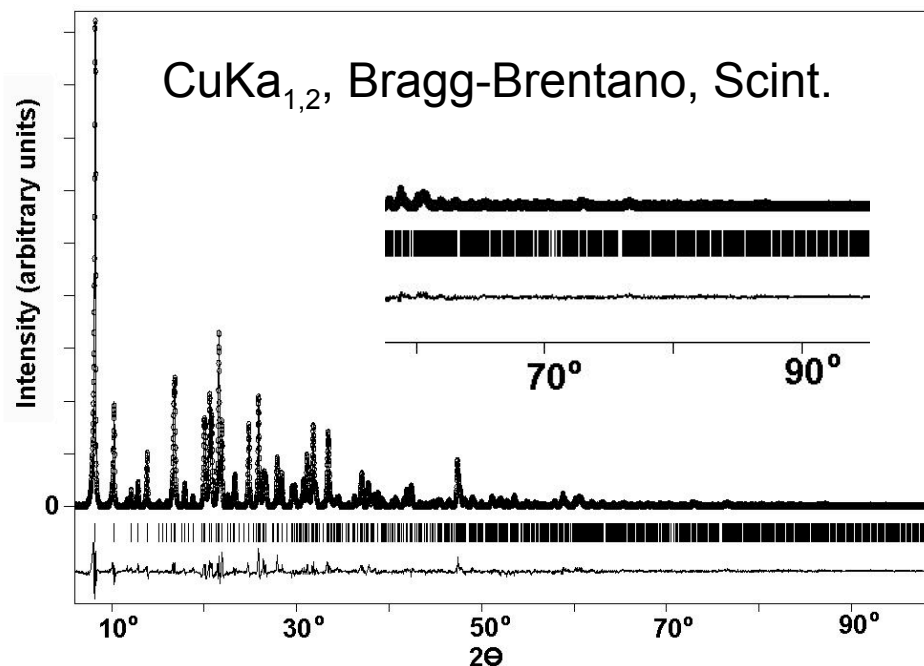
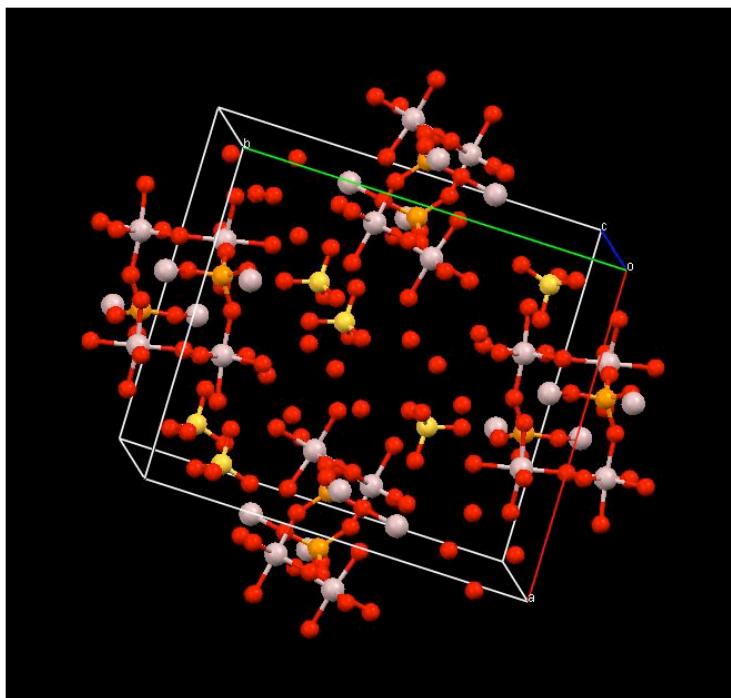
$d_{\min}: 1.3\text{-}1.2 \text{ \AA}$

*E map*



Rius, Elkaim, Torrelles (2004)  
Eur.J. Mineral. 16, 127

# Sanjuanite



Al<sub>2</sub>(PO<sub>4</sub>)(SO<sub>4</sub>)(OH)·9H<sub>2</sub>O, Z= 4,  
 Space group  $P2_1/n$ ,  $V = 1451 \text{ \AA}^3$   
 $a=13.92$ ,  $b=17.24$ ,  $c=6.11 \text{ \AA}$ ,  $\beta=98.3^\circ$

*The Canadian Mineralogist*, **49**, 835 (2011)

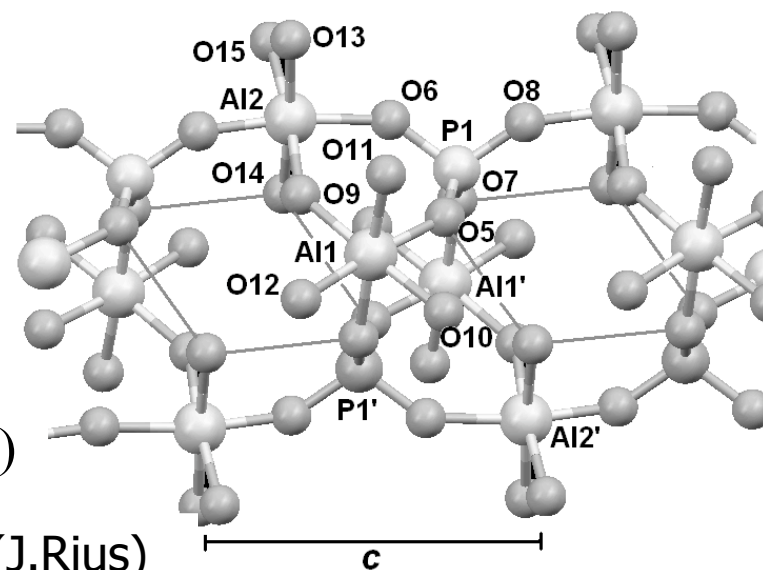


TABLE 1. SUMMARY OF RELEVANT INFORMATION FOR THE RIETVELD REFINEMENT OF SANJUANITE

Unit-cell parameters	
<i>a, b, c</i>	13.9163(5), 17.2422(5), 6.1125(3) Å
$\beta$	98.255(4)°
Unit-cell volume, <i>Z</i>	1450.7(5) Å <sup>3</sup> , 4
Space group	<i>P2<sub>1</sub>/n</i> (#14)
Radiation, wavelength	CuK $\alpha_{1,2}$ , 1.54059, 1.54443 Å
2 $\theta$ range	5.995–100.000°
Number of data points	6268
Peak range in FWHM	20
Number of contributing reflections	1440
Number of profile parameters	10
Number of structural parameters	68
Number of structural restraints	27
Profile function	pseudo-Voigt
Peak breadth	0.13° at 2 $\theta$ = 20°, 0.09° at 2 $\theta$ = 85°
March–Dollase coefficient	1.20(2)
Preferred orientation direction	[ $\bar{2}$ 0 3]
Zero shift	–0.0661(5)°
Background estimation	see Experimental
$R_{wp}$ , $\chi^2$	0.097, 2.47
Weighting scheme	1/ <i>y</i> <sub>o</sub>

TABLE 2. FINAL REFINED COORDINATES OF ATOMS IN SANJUANITE

Atom	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>	Occupancy
S1	0.1264(5)	0.3459(4)	0.4154(16)	1
P1	0.1212(7)	0.0463(6)	0.6855(26)	1
Al1	–0.1099(7)	0.1155(6)	0.5944(22)	1
Al2	0.1809(8)	0.0688(7)	1.2090(25)	1
O1	0.0730(10)	0.3868(8)	0.5733(23)	1
O2	0.1157(10)	0.3795(9)	0.1902(22)	1
O3	0.2312(6)	0.3494(9)	0.5123(30)	1
O4	0.0968(11)	0.2635(5)	0.3956(32)	1
O5	0.1090(13)	–0.0425(8)	0.6397(28)	1
O6	0.1781(13)	0.0826(10)	0.5138(28)	1
O7	0.0276(8)	0.1010(11)	0.6646(40)	1
O8	0.1748(13)	0.0547(12)	0.9249(32)	1
O9	–0.1507(13)	0.0399(8)	0.7903(32)	1
O10	–0.0790(13)	0.1981(10)	0.4080(31)	1
O11	–0.2432(7)	0.1385(11)	0.4860(31)	1
O12	–0.1104(12)	0.1930(10)	0.8185(27)	1
O13	0.3209(9)	0.0524(11)	1.2296(40)	1
O14	0.0469(11)	0.0993(10)	1.1403(40)	1
O15	0.2149(13)	0.1798(9)	1.1860(45)	1
O16	–0.0173(11)	0.3300(9)	0.8685(37)	1.25*
O17	–0.1028(12)	0.4512(9)	0.2361(38)	1.25*
O18	0.3053(11)	0.1940(11)	0.8001(39)	1.25*

TABLE 3. APPROXIMATE BALANCE OF BOND VALENCES (*vu*) FOR SANJUANITE

Atom (X)	S1	P1	Al1	Al2	$\Sigma_c v$	Probable H bonds		O...X...O (°)		
O1	<b>1.50</b>				<b>1.50</b>	– O16	– O17			
	1.48					2.7	3.0			
O2	<b>1.50</b>				<b>1.50</b>	– O11	– O16	– O13		
	1.48					2.5	2.6	3.1		
O3	<b>1.50</b>				<b>1.50</b>	– O12	– O11			
	1.50					2.7	2.8			
O4	<b>1.50</b>				<b>1.50</b>	– O10	– O15			
	1.48					2.7	2.7			
O5		<b>1.25</b>	<b>0.50</b>		<b>1.75</b>	– O14				
		1.56	1.91			2.9				
O6		<b>1.25</b>		<b>0.52</b>	<b>1.77</b>	– O18				
		1.54		1.88		3.0				
O7		<b>1.25</b>	<b>0.50</b>		<b>1.75</b>	– O14				
		1.60	1.92			2.9				
O8		<b>1.25</b>		<b>0.74</b>	<b>1.99</b>	–				
		1.55		1.74						
O9(H)			<b>0.50</b>	<b>0.46</b>	<b>0.96</b>	–				
			1.91	1.92						
O10(w)			<b>0.50</b>		<b>0.50</b>	– O18	– O4			
			1.91			2.5	2.7	104		
O11(w)			<b>0.50</b>		<b>0.50</b>	– O2	– O3			
			1.92			2.5	2.9	121		
O12(w)			<b>0.50</b>		<b>0.50</b>	– O3	– O16			
			1.91			2.7	2.7	126		
O13(w)				<b>0.43</b>	<b>0.43</b>	– O2	– O16			
				1.95		3.1	3.1	114		
O14(w)				<b>0.45</b>	<b>0.45</b>	– O5	– O7			
				1.93		2.9	2.9	120		
O15(w)				<b>0.40</b>	<b>0.40</b>	– O4	– O18			
				1.98		2.7	2.8	137		
O16(w)					<b>0.00</b>	– O12	– O13	– O1	– O2	
						2.7	3.1	2.7	2.6	108
O17(w)					<b>0.00</b>	– O18	– O1			
						2.9	3.0			142
O18(w)					<b>0.00</b>	– O10	– O15	– O6	– O17	
						2.5	2.8	3.0	2.9	108
$\Sigma_A v$	6	5	3	3						

Owing to the expected regularity of their coordination polyhedra and to the large uncertainty in the cation–O distances (s.u.s  $\approx$  0.02 Å), ideal bond-valences  $v_i$  (upper value in bold) are assumed for S1, P1 and Al1; for Al2, they are estimated from the individual Al–O distances  $d_i$  (lower value in Å), with expression  $v_i = K_{Al} d_i \exp(-p_{Al} d_i)$ , where  $p_{Al} = 3.13$  is taken from Rius & Plana (1982) and Allmann (1975), and  $K_{Al} = 98.6$  is fitted to the individual coordination polyhedron to satisfy the charge of Al<sup>3+</sup>. Owing to the low accuracy of the O...O distances (s.u.s  $\approx$  0.1 Å), only the donor (–) or acceptor (–) character of each probable H bond is given. In the last column, the value of the O...X...O angle (°) is listed (except for O16 and O18 in a tetrahedral environment, where it corresponds to the average of the six O...X...O angles).

## Application of DM to organic compounds

DM can cope with molecular compounds, only if intensity data reach **1.1-1.2 Å** resolution. This is the high angle portion of powder patterns where

- 1. peak overlap is most severe,**
- 2. intensity statistics poorer and**
- 3. any inconsistency in the data set (e.g. the variation in unit cell dimensions or radiation damage during data acquisition) is most critical.**

Part of these limitations can be experimentally overcome with a fast read-out solid-state microstrip detector.

## Treatment of peak overlap

The phasing algorithm must be also **capable of handling the very severe peak overlap** of the high-angle region. Patterson-function direct methods<sup>2</sup> is a promising solution for automated solution of molecular compounds.

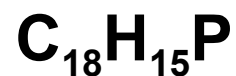
All calculations have been carried out with XLENS\_PD6  
(available at [www.icmab.es/xlens](http://www.icmab.es/xlens)).

<sup>1</sup>Rius, J.; Frontera, C., *J. Appl. Cryst.* **2007**, 40, 1035-1038.

<sup>2</sup>Rius, J. (2011) *Acta Cryst A* **67**, 63-67.

## Example 1

### Triphenylphosphine

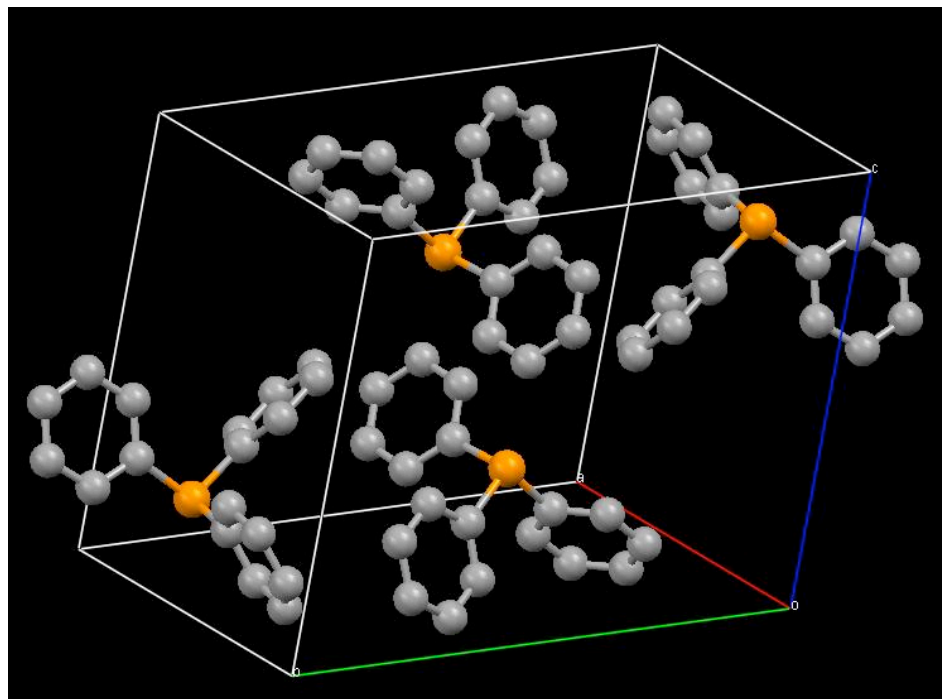


$P2_1/c$

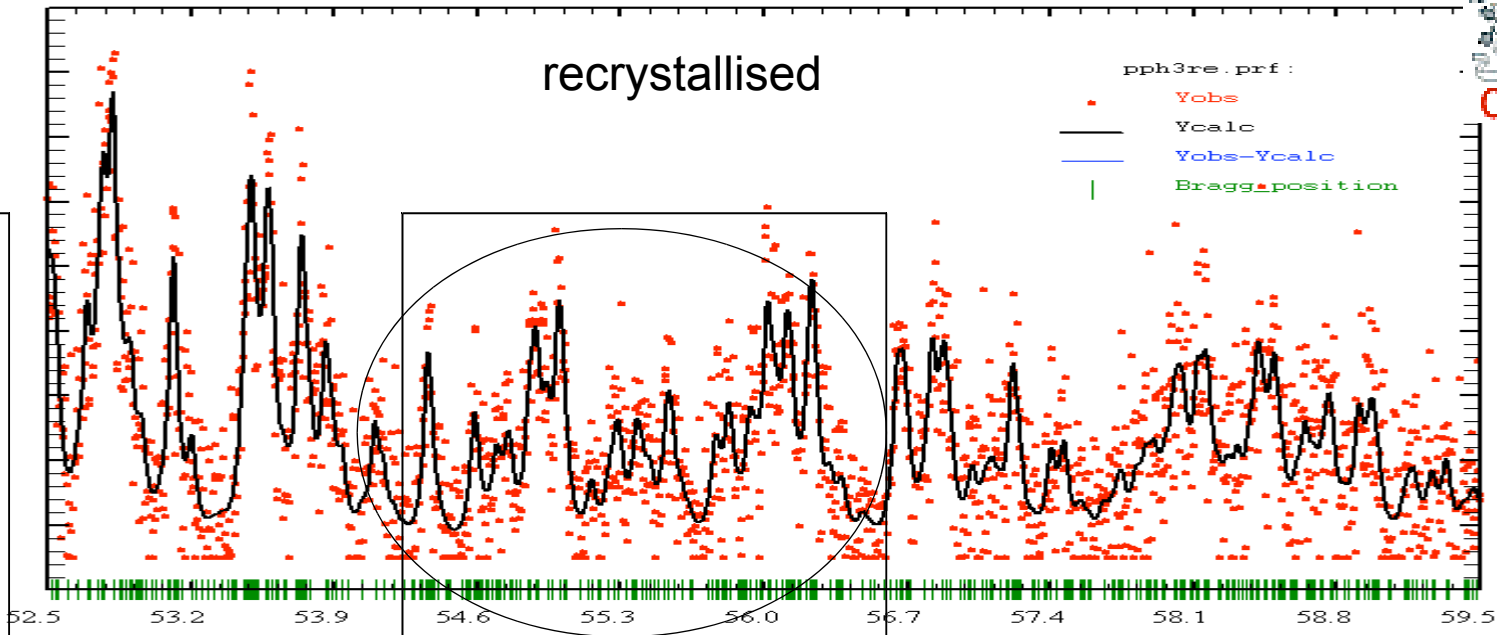
$V = 1460 \text{ \AA}^3$

- 1) As-received from Aldrich
- 2) Recrystallised from hot acetone  
(by Norberto Masciocchi)

Boths sets measured by Fabia  
Gozzo at SLS (Mythen-II detector)



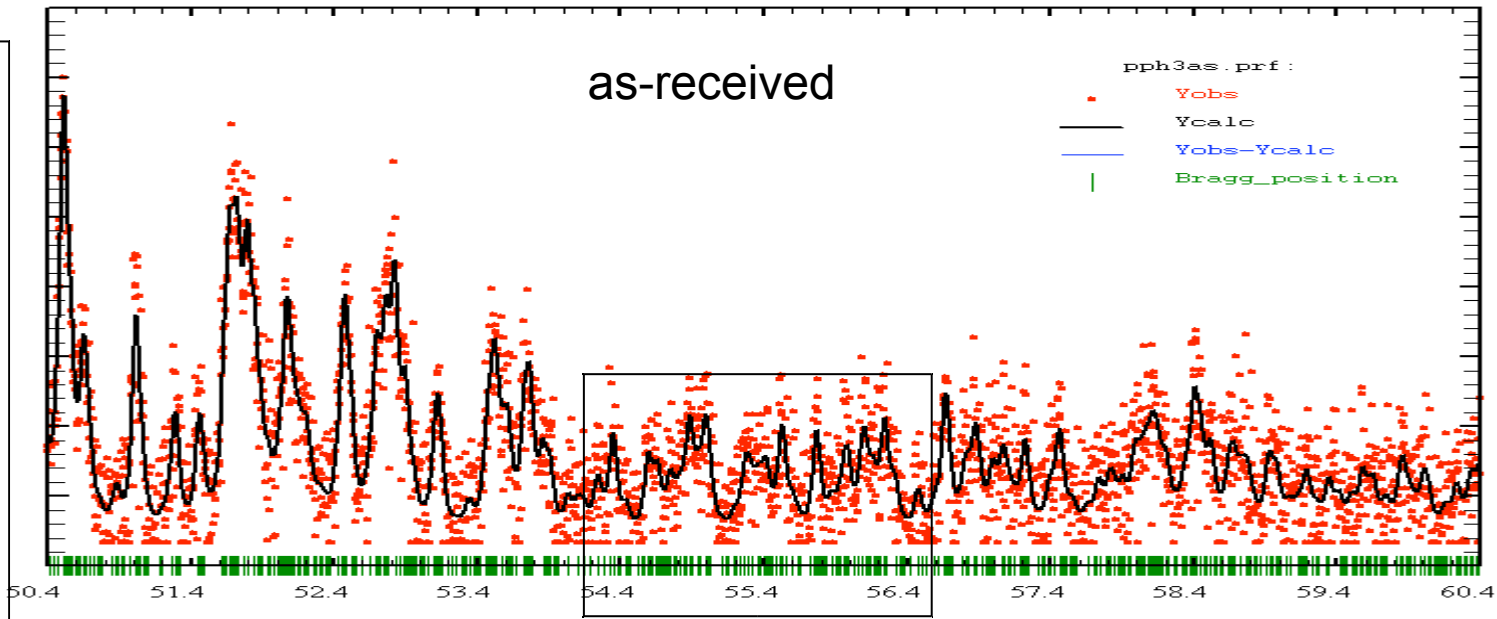
d	FWHM
>5	<0.019
2.5	0.027
1.5	0.040
1.1	0.053
1.0	0.059



d	FWHM
>5	<0.023
2.5	0.035
1.5	0.050
1.1	0.067
1.0	0.075

t = 0.5

25 x FWHM



**XLENS\_PD6 applied to powder data of the recrystallized sample developed the complete model with accurate positions. For the 'as received' sample, the XLENS result is shown below:**

$$d_{\min} = 1.10 \text{ \AA}$$

$$B_{\text{over}} = 4.7 \text{ \AA}^2$$

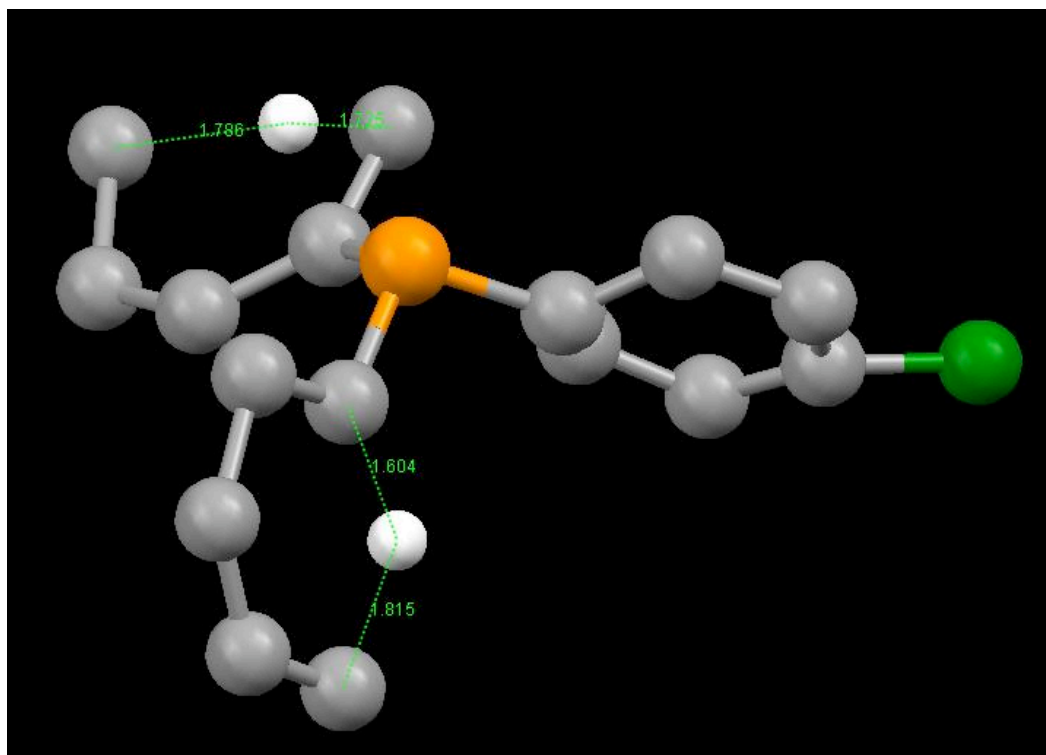
**Success rate = 10 / 50**

**CC<sub>true</sub> : 0.86-0.84**

**CC<sub>wrong</sub> : <0.825**

**N. strong refl. = 320**

**N. refl. (E > 1.15) = 825**





## Example 2

### Structure of (S)-(+)-Ibuprofen from powder data

#### Relevant information:

Chemical name: 2-[4-(2-methylpropyl)phenyl] propanoic acid

Formula of cyclic hydrogen-bonded dimer:  $C_{26} H_{16} O_4$ ,  $Z=2$

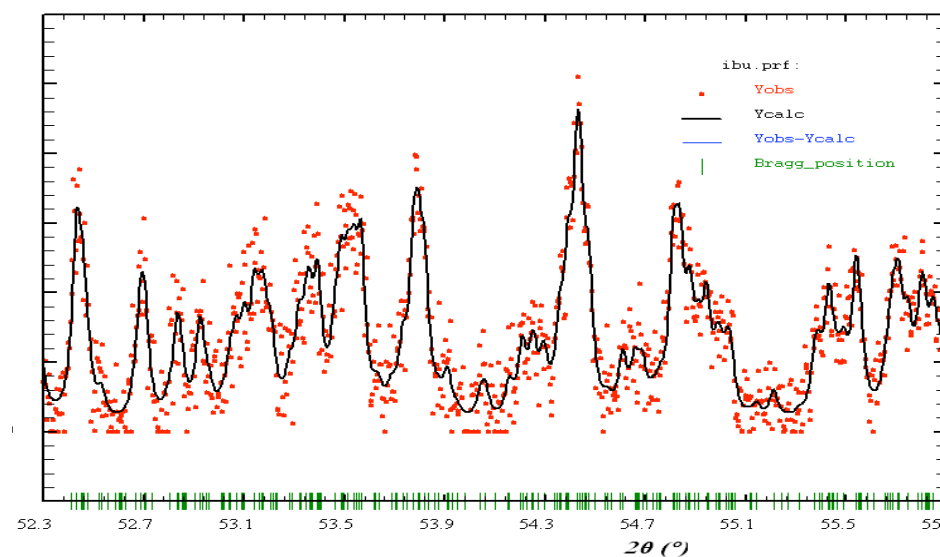
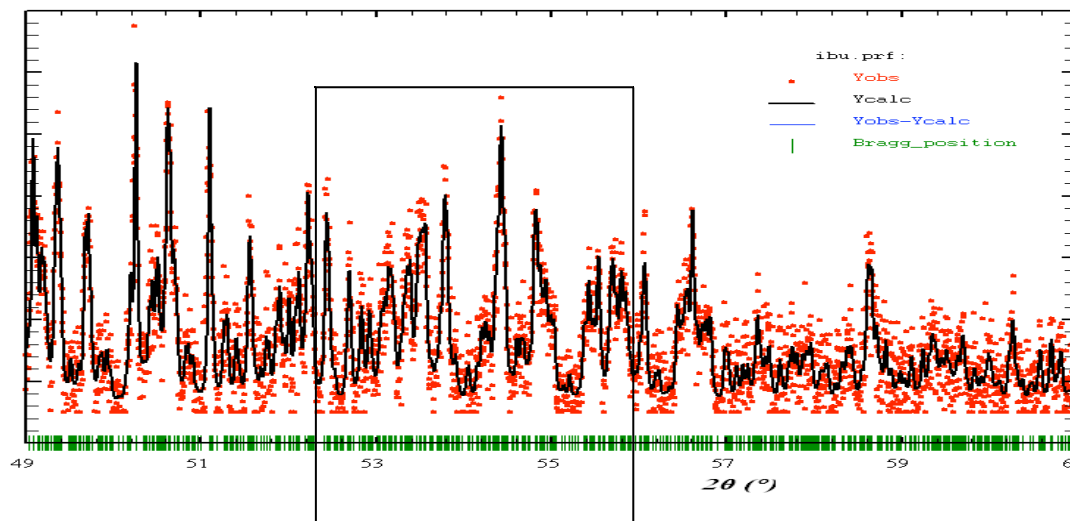
Space group:  $P2_1$

Volume:  $1246 \text{ \AA}^3$

Data measured with MYTHEN-II by F. Gozzo (SLS)

A.FREER\*,J.BUNYAN, N.SHANKLAND AND D. SHEEN. *Acta Cryst.* (1993). C49, 1378-1380

$d$	FWHM
$>10\text{\AA}$	$0.014^\circ$
2.5	0.023
1.5	0.031
1.1	0.040
<b>0.5 x FWHM</b>	
<b>25 x FWHM</b>	
<b>Cauchy prof.</b>	
<b><math>1.00097\text{\AA}</math></b>	



## Summary of DM with XLENS:

$d_{\min} = 1.10 \text{ \AA}$        $B_{\text{over}} = 5.2 \text{ \AA}^2$

Success rate = 7 / 25

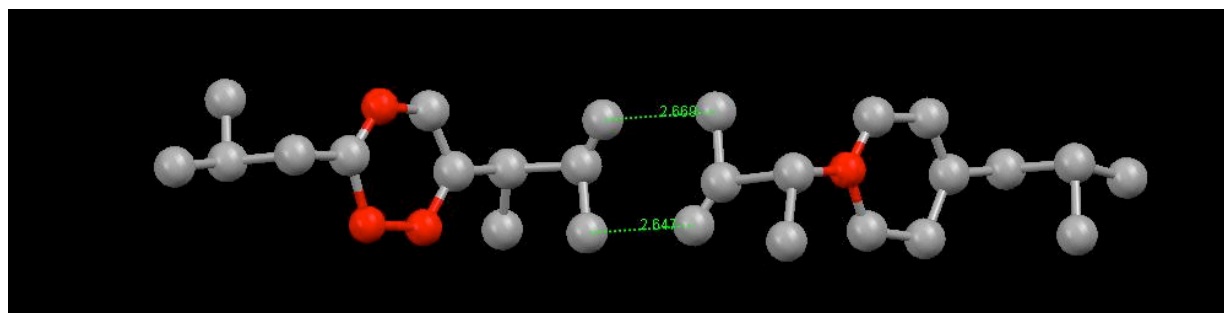
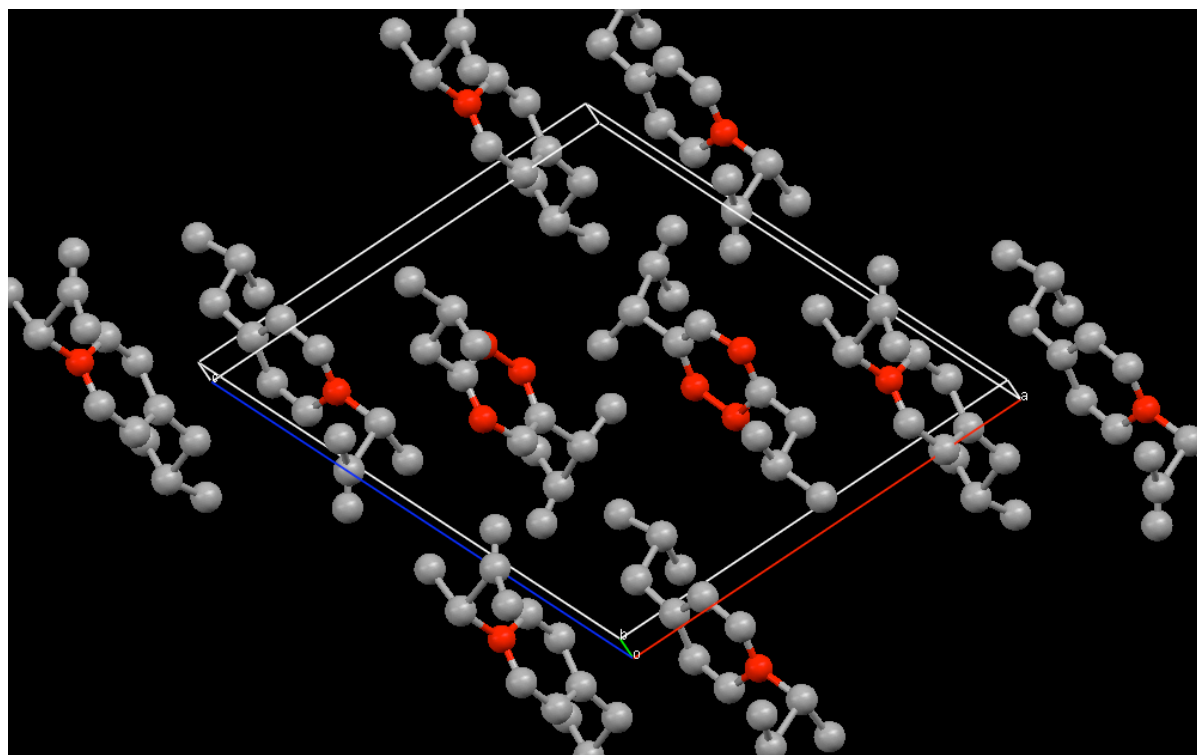
$CC_{\text{true}}: 0.92-0.89$

$CC_{\text{wrong}}:$

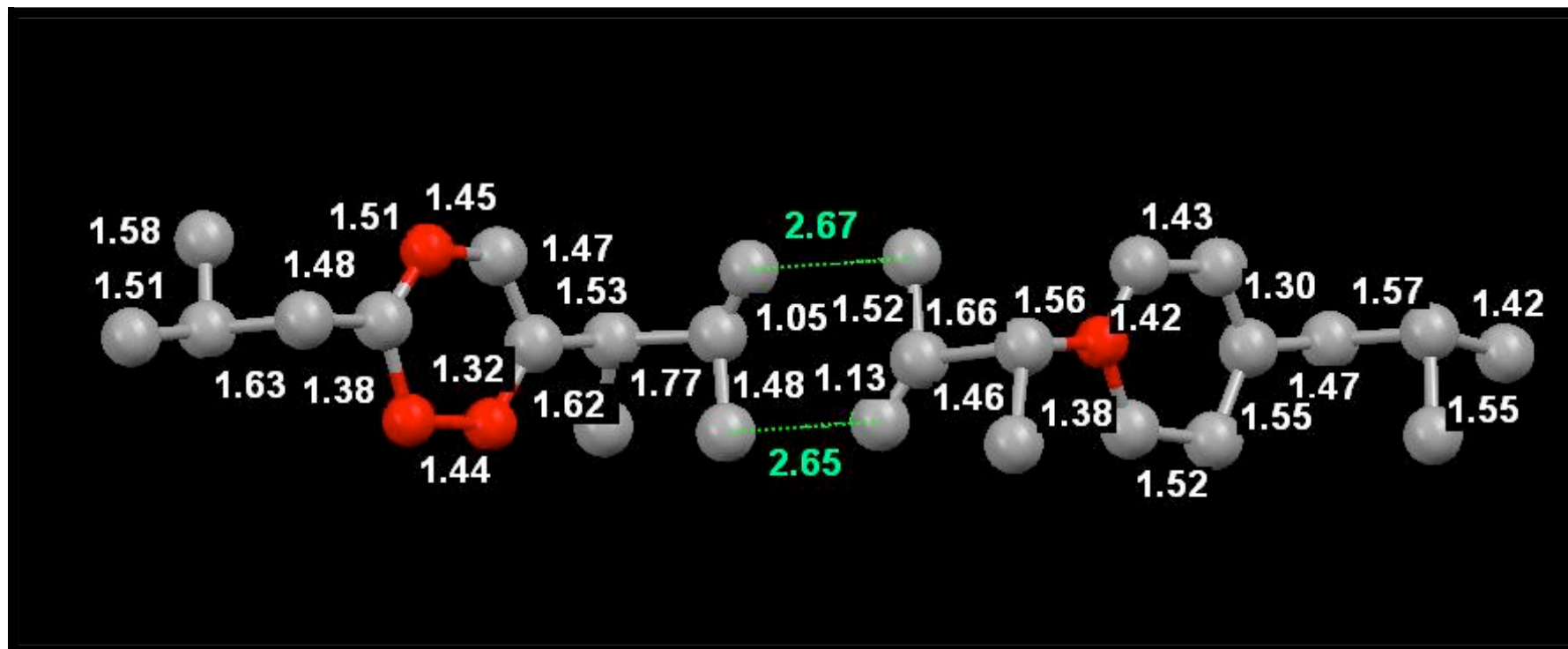
< 0.85

N. strong refl.: 284

N. refl. with E's > 1.15 = 795



# Intramolecular distances directly from DM from powder data



Rius, J. (2011) *Acta Cryst A* 67, 63-67

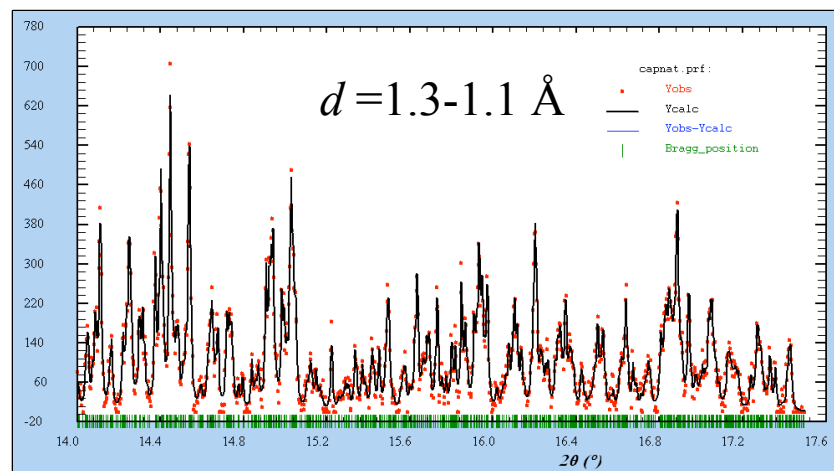
# Calcium hydroxyphosphonoacetate

R.M.P. Colodrero et al. (2011) Cryst. Growth Des. 11, 1713-22



$a=29.72$   $b=8.845$   $c=11.31$  Å  $\beta=93.24^\circ$

$V=2969$  Å<sup>3</sup>,  $I2/a$ ,  $Z=4$



Experimental:

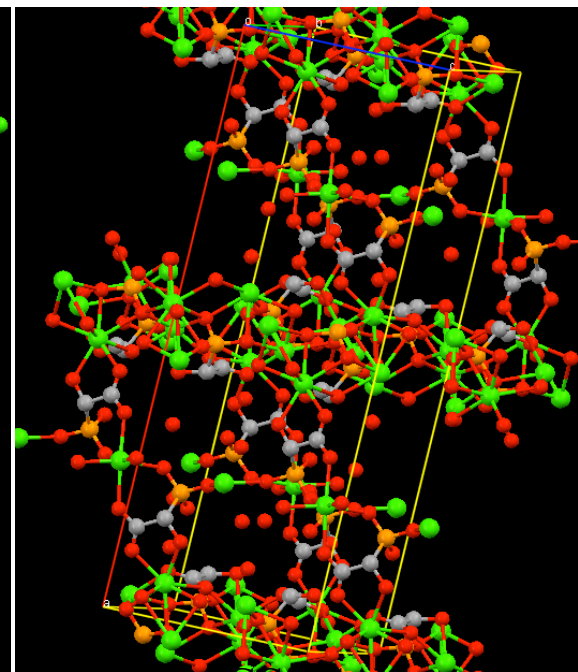
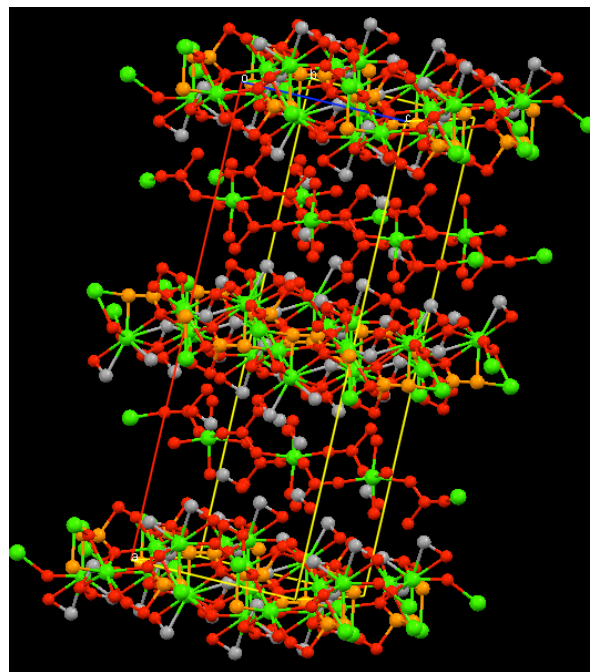
ID31 (ESRF)

$\lambda=0.30$

$2\theta$  from 1.5 to  $20^\circ$

$\Delta=0.003^\circ$  capillary

XLENS<sup>®</sup>\_PD6



GSAS

**Open-Framework Nickel Succinate,  
 $[\text{Ni}_7(\text{C}_4\text{H}_4\text{O}_4)_6(\text{OH})_2(\text{H}_2\text{O})_2] \cdot 2\text{H}_2\text{O}$ : A New  
 Hybrid Material with Three-Dimensional  
 Ni–O–Ni Connectivity\*\***

Paul M. Forster and Anthony K. Cheetham\*

*Angew. Chem. Int. Ed.* 2002, *41*, No. 3

$a = 21.0286$   $c = 45.7728 \text{ \AA}$   $R-3c$   $Z = 18$

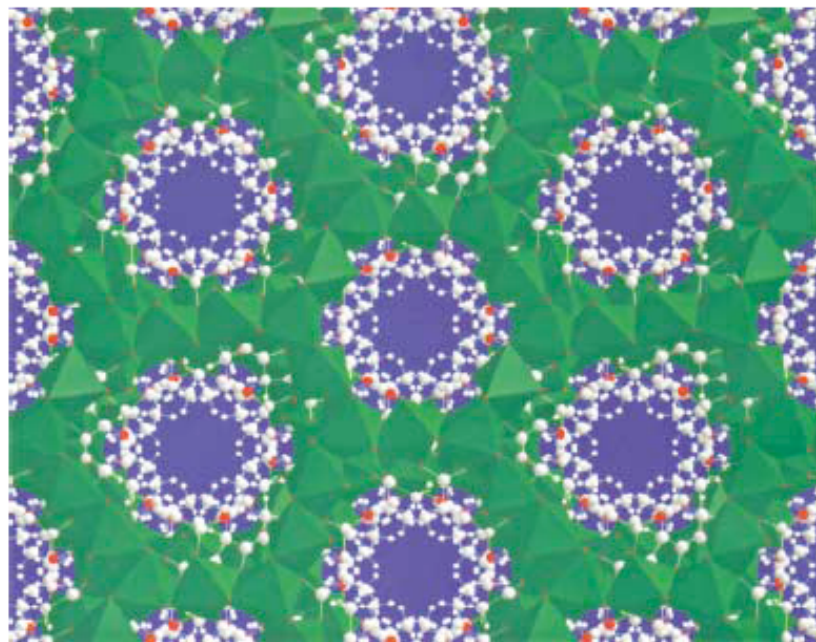
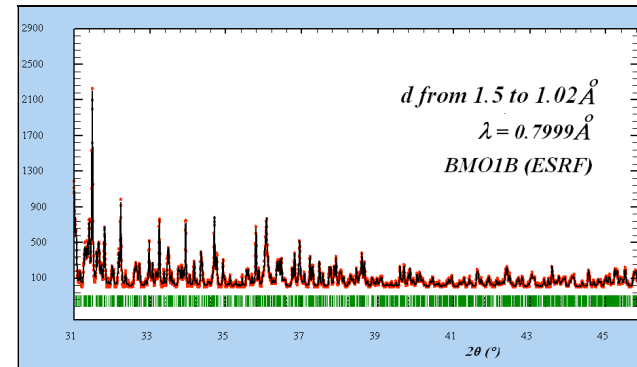
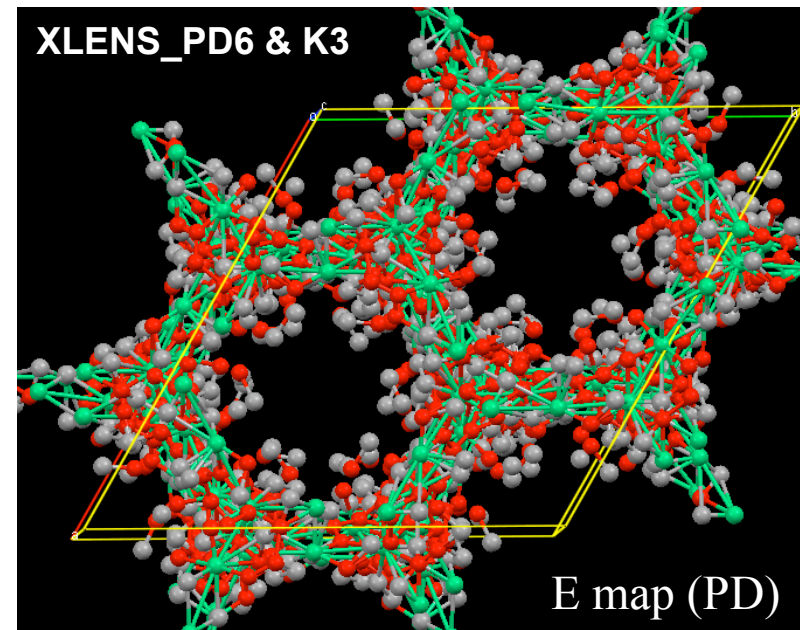


Figure 1. View of the nickel succinate structure down the  $c$  axis.  
 (from single crystal data)



K3 powder data kindly supplied by  
 Dr. Nathalie Guillou  
 Inst. Lavoisier-Franklin  
 Univ. de Versailles (France)



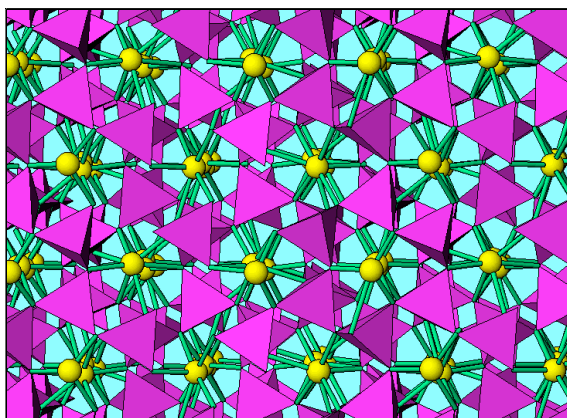
# Patterns with systematic overlap

**limited accidental peak overlap  $\leftrightarrow$  high effective data resolution  
(if systematic peak overlap can be treated)**

**space groups affected by systematic overlap (%):**

- **with cubic lattice: 33%**
- **with tetragonal lattice: 21%**
- **with hexagonal lattice: 65%**

# DM with systematic overlap

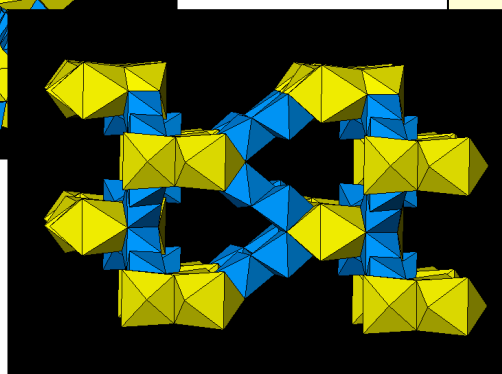
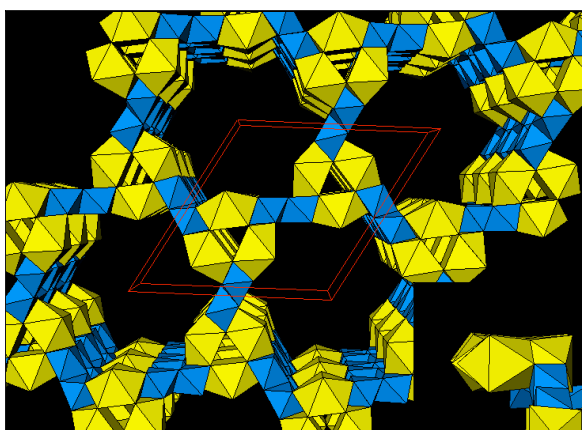


M.Dougill, Nature (1957) 180, 192

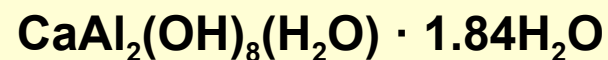
Main phase in High Alumina Cement:  
 $\text{CaAl}_2\text{O}_4$  ( filled trydimite structure type )



hydraulic reaction ( $T < 20^\circ\text{C}$ )



$\text{CAH}_{10}$  (gives strength to set cement) +  
 amorphous content



$$a = 16.387 \quad c = 8.279\text{\AA} \quad V = 1925\text{\AA}^3$$

$$P6_3/m \quad Z=6 \quad \rho_{\text{calc}} = 1.55\text{g/cm}^3$$

30 resolved + 128 syst. overlapped  
 (Lab. data)

Angew. Chem. Int. Ed. (1998) 37 72