The Joint Refinement of Inhibitors of Thermolysin

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Abstract

This chapter will describe preliminary attempts to describe a series of inhibitors jointly, that is, the portions of the protein relatively unaffected by binding must be consistent with all the data sets. The goal is to model the greatest number of observations with the fewest parameters.

The results of this work have applications whenever a set of crystals have similar contents. Such sets occur in inhibitor and mutant studies as well as when solving structures using molecular replacement.

1 Introduction

Quite often a crystallographer will solve a series of almost identical structures. This occurs in the study of an enzymatic mechanism through the use of inhibitor models of reactants, intermediates, or products. The crystallographic procedures used in structure-assisted drug design are practically the same. With the growth of genetic procedures for the production of mutant forms of proteins, it is now quite common for series of similar protein structures to be generated which differ at only one or a few amino acids.

A requirement of this work will be the development of means to model the small nonisomorphisms which will occur from one complex to another. Such a model will be useful in a wide range of applications, from an additional tool in refinement to increase the radius of convergence (a generalization of rigid body refinement) to the optimization of molecular replacement models prior to the solution of the translation function.

The work to be described in this paper has developed out of the continuing project for studying the protease Thermolysin [1]. While Thermolysin is of interest because of its thermostability and its similarity to the angiotensin-converting enzyme neither of these matters will be discussed here.

This paper will discuss the consequences of what appeared to be a very simple decision. It was realized that the model of “native” Thermolysin, which was the starting point for all inhibitor refinement, contained a number of errors. These errors included large torsion angle errors in the side chains of about 5% of the residues in the model and the presence of a dipeptide of unknown composition bound in the active site of the enzyme. Since the model had been built and refined prior to 1981 and no interactive computer graphics were available to aid in the interpretation of the maps, it is perhaps not surprising that such errors were made. It was decided to re-collect the diffraction data for the “native” crystals and refine the model to the current standards for a 1.6Å resolution model.

The additional refinement was completed [2]. The dipeptide was modeled with the sequence val-lys (which is the terminal dipeptide of thermolysin) although there is some evidence in the density map that the contents of the active site are not completely homogenous. The new model contains 185 water molecules (0.6/residue), one DMSO molecule, and 6 side chains with two discrete conformations where the fractional occupancies of each conformation were refined.

The plan was to extract the active site contents of each of the previously refined protein:inhibitor models, place these atoms in the active site of the new “native” model, and remove any atoms in the “native” model which clash with the inhibitor or new solvent atoms. This chimera model was to be the starting model for the updated refinement of the inhibitor.

So much for plans. The first inhibitor complex to be refined was that of the Phosphoramidon inhibitor [3]. The structure of this natural product is Rhamanose-P(O2)-leu-trp. The central phosphoamide group is a mimic of the presumed tetrahedral intermediate of peptide cleavage. While the crystals diffracted quite well, diffraction data were only collected to 2.3Å as that was the limit of the precession photography method used to collect the data. This inhibitor was chosen as a test case for nostalgic reasons and as a limiting case – it and the other precession data inhibitors have the lowest resolution data sets of any of the Thermolysin inhibitors solved so far.

When this inhibitor was refined using the new “native” model as a base the R-value dropped quite low (12 to 13%), but many of the water molecules did not re-
main near their original locations, and the occupancies of the statically disordered side chains were quite misbehaved. The problem with the occupancies is expected for this resolution, and they can easily be fixed at the “native” values. The problem with the wandering solvent is more difficult to solve. This is because the solvent merely haved. The problem with the occupancies is expected for this resolution, and they can easily be fixed at the “native” values. The problem with the wandering solvent is more difficult to solve. This is because the solvent merely exhibits more seriously a general shortcoming of the refinement.

A comparison of the new “native” and the refined thermolysin:phosphorhamidon models shows that many atoms throughout the protein have been shifted by varying amounts. Since the protein does not appear to change overall conformation, outside the vicinity of the active site, one would not expect such alterations to reflect anything other than the greater imprecision of the lower-resolution data set. The low-resolution inhibitor model contains errors which can be identified as such by using the high-resolution data of the “native” crystal but this high-resolution information is not included in the refinement residual.

The traditional means for handling this situation is to impose a “similarity” restraint. The low-resolution model is exposed to the additional restraint that the atoms distant from the active site should be near the location of their mates in the high-resolution model.

There are two major problems with this approach. The first is that similarity restraints, as usually implemented, do not allow much flexibility – literally. If there are cell-constant changes or alterations in the orientation of domains upon binding of the inhibitor, it is not proper to impose the similarity. While this problem is purely an implementation choice and could be generalized, the second problem is more fundamental. The similarity restraint does not embody the basic symmetry of the situation.

Suppose we have a dozen protein:inhibitor data sets we wish to refine. In each case the constant protein part will be restrained to the protein part of the “standard” model. In the end there will be a dozen models, each restrained to their own diffraction data set and the conformation of the standard. But there will be no information passing from one inhibitor to another, even though there are eleven more versions of the protein part to consider. The waste is most evident when the protein:inhibitor crystals diffract as well the “native,” and it especially clear when the “native” is really simply another protein:inhibitor complex.

One would like a method where the high-resolution data from each complex crystal would affect the refinement of all the other complexes.

It is even useful for the data of the lower-resolution crystals to be used in the higher-resolution refinements. In the case of thermolysin, the lower-resolution data sets were collected with the precession film method, and one would expect the precision of these data to be better than the lower-resolution part of the high-resolution oscillation film data sets because of their higher redundancy. In general, as long as the model can handle it, it is always better to use data than to exclude it.

One cannot build this symmetry into the similarity restraints. One could attempt it by building in all the cross-similarities between all the protein parts of the complexes, but some sort of weighting would have to be used to adjust for the differing resolutions of the models. This weighting would be very complicated as it would have to account for the resolution, quality, and completeness of each data set. My rule of thumb is “When the weighting gets tough, you are using the wrong approach.”

2 The Joint Refinement Method

I have chosen to attempt the definition of these restraints as an analog of noncrystallographic restraints. In this approach the model of the protein is segregated in two regions. The first is the region which is essentially unchanged when the inhibitor binds, and the second is the region which does change. During refinement the atoms of the unchanged portion of the model are refined against the diffraction pattern of each inhibitor data set -- there is only one model for all inhibitors. There are independent models for each inhibitor of the variable regions. These atoms are refined in the usual way. If the number of atoms in the variable regions is a small percentage of the total in the crystal, the total number of parameters needed to describe all of the protein:inhibitor complexes will be approximately 1/N that of the parameters used to generate a separate model for each crystal, where N is the number of inhibitors in the joint refinement.

There are two major problems which must be solved when beginning a joint refinement. First, the boundary between the constant and variable regions must be established, and second, the nonisomorphism of the constant region – as it is substituted into each protein:inhibitor crystal – must be modeled. The two problems are connected in that the boundary between the constant and variable regions will depend upon the quality of the nonisomorphism correction.

While the correction for nonisomorphism is the most difficult part of the joint refinement model to construct, it is also quite interesting. Usually protein:inhibitor complexes are refined as independent problems. The result is two sets of coordinates which exhibit a background of variability. It is not easy to examine the two coordinate sets to determine which shifts are significant and which are not. The modeling of nonisomorphism in joint refinement encourages the construction of a model of these differences which requires the fewest parameters. These parameters can be refined with great precision while at the same time the model is
simply not allowed to vary in ways which do not make any improvement in the fit to the observations.

On the other hand, the model of the nonisomorphism is the greatest weakness of joint refinement. It may simply be impossible to generate a model with fewer than a new set of atoms for each new crystal added to the refinement. The existence of a nonisomorphism model cannot be determined from basic principles. One must try to construct a model and decide if the result sufficiently explains the observations.

The overall strategy of joint refinement is:

1) Divide the protein:inhibitor models into constant and variable regions.
2) Design a model of the nonisomorphism of the constant region from crystal to crystal.
3) Refine the joint model against all the diffraction patterns and stereochemical restraints.
4) Compare the joint model, as expressed in each crystal, with the model based on individual refinement. Also compare each joint model with the residual difference map. To correct problems, either move atoms from the constant to the variable part of the model or elaborate the nonisomorphism model.
5) Compare the model of the constant region to the averaged map, and make any required correction. This would include rotating side chains, rebuilding loops, and adding and deleting solvent molecules.
6) Compare the model of the variable region to the map of each crystal.
7) If the model has been changed go to step 3.

(As this paper is principally concerned with the development of the joint refinement method and the modeling of nonisomorphism, steps 5 and 6 were not performed in any of its trial refinements. Refined models described in a paper concerned with the structure and development of nonisomorphism, steps 5 and 6 were not performed in any of its trial refinements. Refined models described in a paper concerned with the structure and function of thermolysin would have to be processed by all these steps.)

Since the number of parameters in a joint refinement is so much smaller than the set of individual refinements, one would expect that the joint model would agree less with the diffraction data. We should not expect the R-values to be as low as those achieved before.

The Mathematics of Joint Refinement

The parameters of a joint refinement model fall into three classes. The first class is the positions, B factors, and occupancies of the atoms in the constant region. These parameters are global in the sense that they affect the model of each and every particular protein:inhibitor complex. These parameters will be identified by the symbol \( c \mathbf{x}_i \), which is the parameter vector for the \( i \)th atom in the constant region. The second class of parameters are the parameters of each atom in each variable region. There is a separate variable region for each crystal. The symbol for these will be \( j \mathbf{x}_i \), where \( j \) is the number of the crystal and \( i \) is the ID number of the atom in that region.

The third class of parameters are of a different type. They are the parameters of the nonisomorphism, and their character will depend on the model of the nonisomorphism. We cannot know their exact form until we have defined the model. In general, however, we can describe the nonisomorphism as a mapping function which takes the general \( c \mathbf{x}_i \) parameters and produces the expression of these atoms in a particular unit cell. This mapping function will be called \( j \mathbf{M}(c \mathbf{x}_i) \). There will be a different mapping function for each crystal \( j \).

Once the atoms of the constant region have been transformed by the mapping function, they can be added to the atoms of the variable region for that crystal, and the resulting coordinate set can be used for the evaluation of the R-value, standard geometry agreement, and refinement gradient calculation just like a normal coordinate set.

To analyze the refinement of a model of this nature let us start with the crystallographic residual. For each crystal the residual is

\[
\sum_{j \mathbf{hkl}} \frac{1}{\sigma^2(\mathbf{hkl})} (F_o(\mathbf{hkl}) - F_c(\mathbf{hkl}, j \mathbf{M}(c \mathbf{x}_i), j \mathbf{x}_j))^2.
\]

To complete the residual, one must combine the contributions of all the crystals. One is tempted to simply sum the individual residuals to get the equation

\[
\sum_j \sum_{j \mathbf{hkl}} \frac{1}{\sigma^2(\mathbf{hkl})} (F_o(\mathbf{hkl}) - F_c(\mathbf{hkl}, j \mathbf{M}(c \mathbf{x}_i), j \mathbf{x}_j))^2.
\]

This is not correct.

The problem is that the residuals — \((F_o - F_c)\) — for each reflection across all the different crystals are not independent. In effect each additional crystal does not provide an amount of information equivalent to that of the first crystal. In the extreme case, if the second crystal provided residuals which were equal to those of the first, no new information would be added by considering it.

We will make the simplifying assumption that the residual for one reflection is independent of the residuals of all the reflections with differing hkl’s. However, for a given hkl the residuals from all the crystals are correlated with each other to some extent. Given this assumption, the form of the total residual is

\[
\sum_{j \mathbf{hkl}} (F_o(\mathbf{hkl}) - F_c(\mathbf{hkl}, j \mathbf{M}(c \mathbf{x}_i), j \mathbf{x}_j))^2 \times \nabla^{-1}(\mathbf{hkl}) \times (F_o(\mathbf{hkl}) - F_c(\mathbf{hkl}, j \mathbf{M}(c \mathbf{x}_i), j \mathbf{x}_j)),
\]
where $V^{-1}(hkl)$ is now a $j \times j$ covariance matrix. (Generally the square root of the variance is defined to be the standard deviation, $\sigma$. Least-squares is usually defined in terms of standard deviations even though the math is more direct when expressed in variances.) The diagonal of $V(hkl)$ contains the variance of the reflection in each crystal while the off-diagonal elements are the products of the standard deviation of each crystal times their correlation coefficient. For a three-crystal joint refinement the variance matrix for a particular reflection would be

$$V(hkl) = \begin{pmatrix} 1\sigma^2 & 1\sigma_1\sigma_{12}r & 1\sigma_1\sigma_{13}r \\ 1\sigma_2\sigma_{12}r & 2\sigma^2 & 2\sigma_2\sigma_{23}r \\ 1\sigma_3\sigma_{13}r & 2\sigma_2\sigma_{23}r & 3\sigma^2 \end{pmatrix}.$$ 

where $\sigma_i$ is the standard deviation of the reflection measured in the $i$th crystal and $r_{ij}$ is the correlation coefficient between the reflection in crystal $i$ and that in crystal $j$.

In practice it is difficult to estimate the individual standard deviations for observed reflections, and it is much harder to estimate all the correlation coefficients. It is much simpler to assume the standard deviation is the same for all crystals and the correlation coefficients are equal as well. This simplification results in the variance matrix

$$V(hkl) = \sigma^2(hkl) \begin{pmatrix} 1 & r & r \\ r & 1 & r \\ r & r & 1 \end{pmatrix}.$$ 

The resulting variance matrix will depend upon the correlation coefficient and the number of crystals in the joint refinement. This relationship is shown in Figure 1.

As can be seen, when the residuals from the crystals are uncorrelated, the least-squares sum simply expands to a sum over the crystals. The contribution of a reflection is the number of crystals. As the residuals become more correlated, the contribution to the least-squares residual drops until, in the limit of a coefficient of one, the contribution of a reflection is independent of the number of crystals.

This relationship is simply a generalization of the notion of “counting statistics.” When you have $N$ independent measurements the variance of the mean is $1/N$ that of a single measurement. If the $N$ measurements are not independent but correlated with a coefficient of one, there is in effect, only one measurement and the variance of the mean is equal to that of a single measurement. Figure 1 shows all the values between.

**Implementation Details**

The ideal implementation of joint refinement would be to write code which would evaluate Equation 1 using an estimate of the correlation coefficient based on an analysis of the diffraction residuals found following separate refinement of every crystal. The correlation coefficient could be estimated as a function of resolution.

Implementing joint refinement in this fashion would be very costly, both in programmers’ time and execution time. The project would require very different code than that existing in TNT [4], the package of choice for this investigator. In addition, computational optimizations such as the real-space calculation of function gradients [5] would not be possible.

For the purpose of testing the viability and utility of joint refinement, several approximations were made to produce a simpler implementation. The joint model consists of a coordinate set containing atoms from the common portion and atoms from each inhibitor. During refinement this coordinate file is expanded (“scattered” in TNT nomenclature) to a separate, complete, coordinate file for each crystal. The least-squares residual function, along with its first derivatives and diagonal elements of the second derivatives, is calculated for each crystal. These derivatives are then collapsed (“gathered”) back into the smaller parameter set by the application of the appropriate transformation for each crystal to the common portion and summing the derivatives.
This implementation is proper only if the residuals are completely uncorrelated. If the residuals are strongly correlated the gradient will be overestimated by a factor of the number of crystals. The diagonal element of the second derivative will, likewise, be overestimated by the same factor. Since the refinement shift is calculated from the ratio of the two, the error cancels.

The cancellation of errors is only approximate because the gradient used to calculate the refinement shift is the sum of the crystallographic term and the stereochemical term and the second derivative is also such a sum. Because the stereochemical validity of the model is determined separately for each crystal, the derivatives of this term are overestimated by a factor of the number of crystals as well. When the residuals are highly correlated, the current method works properly. If the residuals are uncorrelated, this method will not properly balance the crystallographic and stereochemical derivatives. A comparison of the final refined Fo-Fc maps shows that the correlation coefficients of the residuals for these inhibitors are on the order of 0.6.

There is an additional difficulty. Usually the data set from any crystal is not complete. Even though a joint refinement might have six crystals, some reflections might have only been measured five, four, or even fewer times. When this problem occurs, the errors in the crystallographic derivatives and those in the stereochemical derivatives will not cancel. With the current implementation one must be careful to ensure that the areas of reciprocal space covered by the data collection are highly congruent. This limitation results in the requirement that the resolution limits of the crystals' data sets be the same. The original problem of refining a low-resolution model jointly with a high-resolution one cannot be solved with this implementation, but the difficult problem of modeling nonisomorphism can be investigated.

3 Joint Refinement in Practice

To test the feasibility of joint refinement, it was decided to choose a set of thermolysin:inhibitor complexes with the most favorable characteristics. The complexes chosen all diffract to at least 1.7Å and are very similar in structure. In addition the diffraction data for each crystal was collected using the same procedure at about the same time. If joint refinement cannot be made to work for these inhibitors it will never work.

The inhibitors are named ZGPLL, ZGPoLL, ZFPLA, and ZFPoLA [6][7][8]. They can be ordered as a pair of pairs. ZGPLL has the sequence Cbz-Gly-Leu-Leu where the C=O of the peptide bond between the glycine and leucine has been replaced with a PO₂ group to mimic the transition state of the peptide bond cleavage. ZFPLA differs only in that the glycine has been replaced by phenoalinine and the terminal leucine by alanine. In the inhibitors whose names contain the lower-case "o" the amide nitrogen of the central leucine has been replaced with an oxygen.

When the structures of these complexes were originally solved, it was observed that the conformations of each amide-ester pair were nearly identical, but the ZG part binds in a very different conformation from the ZF part of the other inhibitors. This difference in binding caused a small change in the location of a nearby β strand of the protein. While all of the atoms far from the active site differ in location from one inhibitor to another these differences were small and were considered insignificant.

The test of joint refinement was begun by constructing a standard starting model for each crystal. This model contained the new model for “native” and the model of the inhibitor and associated water molecules from the best refinement performed prior to this test. Any water molecules from the “native” model which clashed with the inhibitor were deleted. No attempt was made to manually move any atoms.

For each complex this model was refined in the usual way, 20 cycles with the TNT refinement package [4]. The resolution limit of the diffraction data was 1.7Å, the B factors were allowed to vary without stereochemical restraint, and the group occupancies of the disordered side chains and the inhibitors themselves were allowed to vary. For simplicity’s sake, no manual evaluations of the resulting models were made. The R-values of the resulting models are given in the first column of Table 1.

The first test of joint refinement was made with no attempt to model nonisomorphism. Three refinement runs were performed. The inhibitors were joined pairwise and then all together. To allow for the adjustment of the protein due to inhibitor binding, residues 111 through 119, 143, and the zinc atom were modeled with separate copies for each crystal, along with the inhibitor itself and the associated water molecules. In ZGPLL and ZGPoLL an additional DMSO molecule binds near the inhibitor, and this molecule was treated as inhibitor-associated solvent.

A number of details must be considered when performing this refinement. The most important is that the overall B factor of all but one of the crystals in a refinement must be allowed to vary. In general one should also allow for varying the overall anisotropic B factor, but this was not done in this case because the diffraction decayed very similarly in all cases.

Initially the crystals were refined pairwise. This seemed to be the most ideal arrangement because the two “ZG” inhibitors and the two “ZF” inhibitors are very similar to one another. The R-values in Table 1 show that the resulting model for the “ZG” inhibitors generates agreement with the individual diffraction data sets almost as well as the individual models. The “ZF” models lose about four tenths of a percent of R-value in each case, which is slightly worse than the “ZG” joint refinement.
The agreement of the resulting models with the diffraction data shows a small decrease in the quality of the fit when the “ZG” variants are joined, and again a small decrease with the joined “ZF” variants, but a large drop in quality when all four are joined. This pattern implies that the two types of inhibitors are in some sense incompatible.

The decrease in the fit of the models to the data could arise from the large decrease in the number of parameters. The models for four crystals refined independently contain about 40,000 parameters which are defined by refining against about 100,000 diffraction intensities. The four-fold joint model, however, contains only about 10,000 parameters. One might expect the R-values to rise for this reason alone. Of course the R-value may be rising because of a failure to model the nonisomorphism. If this is the case the model should be updated.

The only way to be sure which possibility is the cause is to examine the joint model against the difference maps and compare the individual models. One expects an atom in the joint model will lie in the center of the distribution formed by the corresponding atoms from the individual models. The significance of the breadth of the distribution is judged based on the size of the difference map features.

Such an examination shows a number of regions where it appears that strands of polypeptide chain are displaced relative to one another. Apparently there are small changes in the location and orientation of each domain. To model this motion, it was decided to allow the two domains to move as rigid bodies from one inhibitor to another.

The thermolysin molecule consists of two domains. Residues 1 through 125 form the N-terminal domain and 126 to 316 form the C-terminal domain. The water molecules and metal ions were each associated with the domain they lay closest to. The rigid-body shifts of these domains were determined by comparing the orientation of the domains in the “native” model with each individually refined protein:inhibitor model.

Table 2 lists the R-values for each model, refined with allowance for domain motion. The increase in R-value upon imposing a two-fold joint refinement is slightly less than before but the table shows great improvement for the four-fold joint refinement. Where before the R-values increased by 1.1 to 1.8%, the increase is now only ranges from 0.5 to 0.8%.

This result implies that there is a significant rigid-body shift of the two domains of thermolysin upon binding of some inhibitors. Although the shift does occur and is present in the previously refined models, it was never recognized because of its small size. These shifts were simply considered part of the “background” shifts of the individual atoms in the model.

When these models are examined, it is apparent that some bulk shifts of regions of each domain are still unmodeled. Since these regions appear to be near the crystal contacts the possibility that the cell constants of each crystal differ was investigated.

### 4 Cell Constant Precision

The oscillation film data reduction software [9][10] is not considered a reliable source of cell constant information. Because the diffraction data sets for most high-resolution thermolysin:inhibitor complexes were processed using this software, it was decided to refine all inhibitors of thermolysin using the cell constants of the “native” crystal as determined from precession photographs. While it is believed that the cell constants of the crystals do change upon inhibitor replacement, test calcu-
lations showed that the quality of the refined model is insensitive to errors in cell constants. The cell lengths can be varied by 2% and not significantly degrade the agreement of the model with the diffraction intensities and the stereochemical restraints.

Joint refinement should be sensitive to differences in cell length from one inhibitor to another. If the cell lengths are defined to be equal for all crystals, one will observe that the contents of one crystal might shrink and other swell. These changes cannot be accommodated using the rigid-body motions of the refinements reported in Table 2.

To test for this possibility, a more generalized noncrystallographic symmetry transformation was developed. Instead of insisting that the matrix applied to the coordinates be a rotation matrix, a general matrix was allowed. Such a matrix introduces a resizing of the domain as well as a rotation. While this model can accommodate cell constant changes, it is much more general and will correct for other types of differences between the two models. If this model of nonisomorphism fails to improve the fit of the joint model, cell constant errors are not significant, but if this model is successful, the cause might not be due to the modeling of cell constant errors.

The refinement programs were modified to relax the constraints on the noncrystallographic symmetry operators. The transformations were again derived by comparing the “native” model with the individually refined models of the protein:inhibitor complexes, and the joint refinements were processed again. The changes in the final R-values, relative to those in Table 2, are listed in Table 3.

As seen in the table, the R-values did not drop significantly. This implies that errors in the measurement of the cell constants are not important determinants of the results of this joint refinement.

### 5 Quadratic Transformations

Since a visual comparison of the four-fold joint refinement models and the individually refined models show bulk displacements of certain regions of each domain, some form of mapping of the “prototypical” domain onto each crystal’s instance more general than a rotation and translation is required. A transformation which allows for differing rotations for different portions of the domains is required. The next logical step is to attempt quadratic transformations [11] (simple rotations are linear transformations).

Quadratic transformations are third-order tensors which are vector-multiplied by the position vector of an atom to generate a rotation matrix which is again multiplied by the position vector to generate the new location of the atom. They are difficult to express in vector-matrix notation – I will use a boldface capital letter with a dot over it to represent these quantities.

The expression for a quadratic transformation is

\[ x' = t + Rx + \frac{1}{2} x^T \mathbf{D} x \]

\( \mathbf{D} \) is a 3x3x3 symmetric tensor and therefore contains 18 unique elements. A model for nonisomorphism such as this will require 24 parameters for each domain.

The implementation of this model is being constructed.

### 6 Summary

The mathematical basis for joint refinement has been developed, and several models for the small nonisomorphisms between members of a set of protein:inhibitor complexes have been tested. It has been demonstrated that the data from four crystals can be modeled with nearly \( \frac{1}{4} \) the usual number of parameters with no more than 0.8% increase in the R-value.

With a suitable model for the nonisomorphism, the quality of the fit should improve. It does not appear unreasonable to expect that one could construct a joint model which agrees with the observations from each crystal as well as a model constructed specifically for that crystal.

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Table 3 Decrease in R-Value Caused by Allowing Proteins to Rescale in Size. The noncrystallographic symmetry transformation was generalized to allow for a change in scale as well as a rotation and translation and the joint refinements repeated. Each entry shows the change in R-value between the resulting models and the R-values in Table 2. Very little improvement resulted.
7 Acknowledgment

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References

[8] Unpublished results. The structure of ZFPoLA.