Total Scattering and PDF analysis of nanostructured materials

S.J.L. Billinge

Department of Applied Physics and Applied Mathematics Columbia University, CMPMS, Brookhaven National Laboratory







Complex materials

- Photovoltaics with improved efficiency
 - Nanoparticles in the light collecting layer
- High energy density batteries
 - Electrodes
 - Electrolytes
- Fuel cells for transportation applications
 - Electrodes
 - Electrolytes
 - Catalysts
 - Hydrogen storage

Sequestration

Functionalized mesoporous materials

THEGR

U. Uppsala

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The Nanostructure Problem

• We want to engineer materials at the nanoscale

• But we can't even solve the atomic structure at the nanoscale:

The nanostructure problem







Total scattering ?

Cross section of 50x50x50 u.c. model crystal consisting of 70% black atoms and 30% vacancies ! Properties might depend on vacancy ordering !!





Bragg peaks are blind ..



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Diffuse scattering to the rescue ..



Diffuse scattering: Information about two-body correlations, i.e. chemical short-range order or local distortions.







How about powder diffraction ?



Finally the Pair Distribution Function



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The PDF is the Fourier transform of the total scattering diffraction pattern !

Proffen, Z. Krist, 215, 661 (2000)

The atomic Pair Distribution Function



What is the PDF?

•Sit on an atom and look ⇒ at your neighborhood

•*G*(*r*) gives the probability of finding a neighbor at a distance *r*

•PDF is experimentally accessible

•PDF gives the local structure







But there is no information at high-Q...?



Computational issues: A Brief History of PDF



• Pieter Debye, 1915:

$$I = \sum_{n} \sum_{m} f_{m} f_{n}^{*} \frac{\sin qr_{mn}}{qr_{mn}}$$

• Fritz Zernike and Jon Prins, 1927:

$$4\pi r^2 \rho(r) = 4\pi r^2 \rho_a + \frac{2r}{\pi} \int_0^\infty q i(q) \sin q r dq$$









History

Debye and Menke, Z. Phys. (1930)

PDFs of mercury

Tarasov, L. P., and Warren, B. E., (1936) *J. Chem. Phys.*, **4**, 236.

X-ray PDFs of molten sodium









The Atomic Pair Distribution Function (PDF) Method

- Use modern high intensity x-ray and neutron sources to collect unprecedentedly precise data
- Utilize all the information: Bragg and diffuse scattering
- Use modern computing capabilities to analyze, model and visualize the data





- Chupas et al., J. Appl. Crystallogr. (2003)
- Billinge-group, BNL, SUNY-SB, APS collaboration
- Main developments thanks to Pete Chupas and Xiangyun Qiu

X-ray PDF measurements

Area detector setup at high energy synchrotron beamlines.

• Fast (30 Hz)



Single/Multi energy dispersive detector setup.

- Slow (hours)
- Very high Q resolution



Laboratory diffractometers

- Feasible with Mo or Ag radiation
- Limited Qmax
- Slow (hours)







Synchrotron beamlines for PDF work

- NSLS-II @ Brookhaven National Laboratory
 - XPD
 - XPD-2 (under construction)
- APS @ Argonne National Laboratory
 - 11IDB, 11IDC
- ESRF
 - ID15, ID11, ID22
- Spring 8
 - various
- DESY
 - P07
- Diamond
 - XPDF (undergoing commissioning)





X-ray PDF: In-house measurements







RAPDF with Neutrons



POWGEN3 & NOMAD @SNS

D4 @ILL





PDFs from laboratory microscopes



Zeitschrift für KristallographieCRYSTALLINE
MATERIALS



Volume 227 5/2012

Analysis of Complex Materials

Edited by Thomas Proffen and Reinhard B. Neder

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Au (1000) Å particles



	ePDF (film)	ePDF (NP)	xPDF
Q_{\max} (Å ⁻¹)	15.25	15.25	15.25
Fit range (Å)	1 - 20	1-20	1 - 20
Cell parameter (Å)	4.075(3)	4.076(2)	4.058(1)
$U_{\rm iso}$ (Å ²)	0.033(4)	0.006 (3)	0.014(1)
Diameter (Å)	$\sim 27^a$	$\sim 1000^{b}$	24.51(9)
Q-damp (Å ⁻¹)	0.095(5)	0.095(5)	0.047(2)
<i>Rw</i> (%)	17	24	20

a: film thickness measured during deposition

b: NP diameter estimated directly from the TEM image



ePDFsuite software. Ask for details

(c)

(d)

18

20

Nanostructure refinement



Modeling summary

- Small Box modeling
 - Similar in nature to Rietveld refinement of powder diffraction data
 - Small number of parameters, highly constrained fits
 - Danger of model bias, difficult to find distorted solutions.
 - Exemplars: PDFgui
- Large Box modeling
 - Large number of atoms in a box allowed to move around to each and the
 - Small number of constraints, exploratory unbiased fittin distorted solutions
 - Danger of overfitting and degenerate solutions. Difficult uncertainties
 - Exemplars: RMCprofile, RMC and Diffev in DISCUS, E
- George Box modeling
 - All models are wrong; some models are useful.
 - George E. P. Box, William Hunter and Stuart Hunte *Experimenters*, second edition, 2005, page 440.

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PDFgui

Used to be called "real-space Rietveld"

- Starting point is a crystallographic description of the model
- Small Unit cell, periodic boundary conditions
- Fits to G(r) which is the FT of F(Q)
- PDFgui
 - Available from diffpy.org
 - Development funded by NSF-DANSE program







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	sratio	o 1.0	r	cut 0.0		step	ocut	0.0								
	Included Pa	_{airs} all-all														
	elem	x y z	u11	u22	u33	u12	u13	u23	occ							
	1 Pb (0.5 0.5 0.5	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0							
Plot Control X	2 Pb (0.5 0.0 0.0	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0							
X	3 Pb (0.0 0.5 0.0	0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0							
step 👻	4 Pb (0.0186431	0.0186431	0.0186431	0.0	0.0	0.0	1.0							
Y	6 Se (0.0 0.5 0.5	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0							
	7 Se (0.5 0.0 0.5	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0							
lat(1)	8 Se (0.5 0.5 0.0	0.0143116	0.0143116	0.0143116	0.0	0.0	0.0	1.0							
lat(2)																
lat(3)																
pscale																
u11(1)																
u11(2) +																
offset -5																
Plot Reset											 					
PDEfit2 Output																





PDFfit2 Output

CMI: complex modeling infrastructure

• CMI

- Also available at diffpy.org
- Very powerful
- Very difficult to use
- We are working on a more friendly user interface and better documentation, but for now it is advised to contact us and we can help you get started







Diffpy-Complex Modeling Infrastructure: Diffpy-CMI

Signal Community Publications Products -

DiffPy-CMI

DiffPy-CMI is our complex modeling framework. It is a highly flexible library of Python modules for robust modeling of nanostructures in crystals, materials.

The software provides functionality for storage and manipulation of structure data and calculation of structure-based quantities, such as PDF, SA overlaps, bond lengths, and coordinations. Most importantly the DiffPy-CMI package contains a fitting framework for combining multiple experime problem.

This is an early release of code that is under intense development, with support for installation on Unix, Linux, and Macintosh machines. The soc will evolve rapidly, but we want to make the code available at the earliest possible date. Please make use of the software and provide feedback a but please be patient and check back frequently for updates.





```
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◀ ►
       untitled
                         •
       import numpy as np
       import pylab
       from scipy.optimize.minpack import leastsq
       from diffpy.Structure import loadStructure
       from diffpy.srfit.pdf import PDFContribution
       from diffpy.srfit.fitbase import FitRecipe, FitResults
       dataFile = "ni-q27r100-neutron.gr"
      structureFile = "ni.cif"
       spaceGroup = "Fm-3m"
      niPDF = PDFContribution("nickel")
      niPDF.loadData(dataFile)
      niPDF.setCalculationRange(xmin=1, xmax=20, dx=0.01)
       niStructure = loadStructure(structureFile)
      niPDF.addStructure("nickel", niStructure)
       niFit = FitRecipe()
      niFit.addContribution(niPDF)
```

Line 107 Column 1

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```
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< >
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       niFit.clearFitHooks()
       print "Refine PDF using scipy's least-squares optimizer:"
       print " variables:", niFit.names
       print " initial values:", niFit.values
       leastsq(niFit.residual, niFit.values)
       print " final values:", niFit.values
       print
       niResults = FitResults(niFit)
       print "FIT RESULTS\n"
       print niResults
       r = niFit.nickel.profile.x
       gobs = niFit.nickel.profile.y
       gcalc = niFit.nickel.evaluate()
       baseline = 1.1 * gobs.min()
       gdiff = gobs - gcalc
       pylab.figure()
       pylab.plot(r, gobs, 'bo', label="G(r) data",
               markerfacecolor='none', markeredgecolor='b')
       pylab.plot(r, gcalc, 'r-', label="G(r) fit")
       pylab.plot(r, gdiff + baseline, 'g-', label="G(r) diff")
 100
       pylab.plot(r, np.zeros_like(r) + baseline, 'k:')
       pylab.xlabel(r"r ($\AA$)")
       pylab.ylabel(r"G ($\AA^{-2}$)")
       pylab.legend()
 104
 105
       pylab.show()
```

Diffpy project (BNL LDRD) Complex Modeling infrastructure: Diffpy-CMI

Official release of Diffpy-CMI v0.1

www.diffpy.org



DiffPy - Atomic Structure Analysis in Python

A free and open source software project to provide python software for diffraction analysis and the study of the atomic structure of materials.



Nanomaterials











The Nanoparticle structure problem

1. Powder of similar but not identical powders

- 1. Structure
- 2. Defects
- 3. TD properties Pt NPs







Quantum Dot solar cells



CdSe quantum dots



- RAPDF experiments at APS, Sector 6
- Work of grad student Ahmad Masadeh

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• Masadeh, SJB et al. PRB 76, 115413 (2007)

H

а

Structure of the CdSe core



• Wurtzite structure



• Zinc blende structure





Masadeh, SJB *et al.* PRB **76**, 115413 (2007)

Thanks to Reinhard Neder for help with stacking fault models

	CdSe-l	oulk	CdSeIII		CdSeI.	[CdSeI	
Stacking fault density (%)	0.0	33.0	0.0	50.0	0.0	50.0	0.0	50.0
a (Å)	4.3014(4)	4.3012(4)	4.2997(9)	4.2987(9)	4.3028(9)	4.3015(9)	4.2930(9)	4.2930(8)
c (Å)	7.0146(9)	7.0123(9)	7.0145(4)	7.0123(4)	6.9987(9)	6.9975(9)	6.9405(9)	6.9405(7)
Se Z-frac.	0.3774(3)	0.3771(3)	0.3761(9)	0.3759(9)	0.3751(6)	0.3747(6)	0.3685(9)	0.3694(9)
$Cd U_{11} = U_{22} (Å^2)$	0.0108(2)	0.0102(2)	0.0146(7)	0.0149(7)	0.0149(6)	0.0112(5)	0.0237(9)	0.0213(8)
U ₃₃ (Å ²)	0.0113(3)	0.0112(3)	0.0262(9)	0.0241(9)	0.0274(9)	0.0271(9)	0.0261(9)	0.0281(9)
Se $U_{11} = U_{22} (Å^2)$	0.0109(9)	0.0102(9)	0.0077(7)	0.0138(7)	0.0083(7)	0.0121(7)	0.0110(9)	0.0191(9)
U ₃₃ (Å ²)	0.0462(9)	0.0115(9)	0.1501(9)	0.02301(9)	0.1628(9)	0.0265(9)	0.1765(9)	0.0311(9)
NP ^a diameter (nm)	∞	∞	3.7(1)	3.7(1)	3.1(1)	3.1(1)	2.4(2)	2.2(2)
R_w	0.12	0.09	0.20	0.14	0.18	0.15	0.27	0.21

Size of the structural core



$$f\left(r,d\right) = \left[1 - \frac{3r}{2d} + \frac{1}{2}\left(\frac{r}{d}\right)^3\right]\Theta(d-r),$$

• Masadeh, SJB et al. PRB 76, 115413 (2007)

• Also see Shamoto paper, JAC 2007

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TABLE I: CdSe nanoparticle diameter as determined using various methods.

	CdSeIII	CdSeII	CdSeI
Nucleation time (s)	1200	630	15
Diameter (nm)			
TEM	3.5(2)	2.7(2)	2.0(2)
UV-vis	3.5(4)	2.9(3)	≤ 1.90
PL	3.6(4)	2.9(3)	≤ 2.1
PDF	3.7(1)	3.1(1)	2.2(2)

White Light Nanoparticles

BROO



 Xiaohao Yang, Masadeh, McBride, Bozin, Rosenthal and SJLB, *Phys. Chem. Chem. Phys.* 15, 8480-8486 (2013)





Zr/Sn phenyl phosphate, unconventional MOFs





Clearfield, A. Dalton Trans. 2008, 44, 6089-6102.

- Collaboration with the group of Abe Clearfield, Texas A&
- Work of Chenyang Shi and Rita Silbernagel

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Try ZrP structures on H-Zr sample, PDFgui



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 Use PDFgui to fit 3D crystal structures from the literature (as indicated)







Structure solution from PDF





Example: DFT can predict structures

- DFT is one of the most accurate of the theories (but still approximate)
- This is the basis of Materials Prediction, a fundamental of Materials Genomics
- Can DFT predict the stable structure of Au nanoparticles?
 Yes!







Published on Web 09/02/2009

Thiolate-Protected Au₂₀(SR)₁₆ Cluster: Prolate Au₈ Core with New [Au₃(SR)₄] Staple Motif

Yong Pei, Yi Gao, Nan Shao, and Xiao Cheng Zeng*

Department of Chemistry and Nebraska Center for Materials and Nanoscience, University of Nebraska-Lincoln, Lincoln, Nebraska 68588



Published on Web 04/12/2008

Correlating the Crystal Structure of A Thiol-Protected Au₂₅ Cluster and Optical Properties

Manzhou Zhu,[†] Christine M. Aikens,[‡] Frederick J. Hollander,[§] George C. Schatz,^{II} and Rongchao Jin^{*,†}



J|A|C|S

Published on Web 06/01/2010

Total Structure Determination of Thiolate-Protected Au₃₈ Nanoparticles

Huifeng Qian,[†] William T. Eckenhoff,[‡] Yan Zhu,[†] Tomislav Pintauer,[‡] and Rongchao Jin^{*,†} Department of Chemistry, Carnegie Mellon University, Pittsburgh, Pennsylvania 15213 and Department of Chemistry and Biochemistry, Duquesne University, Pittsburgh, Pennsylvania 15282



DFT study of Au₁₄₄ structure



Icosahedral core

Au/S surface structure with ligand attachment



Structure and Bonding in the Ubiquitous Icosahedral Metallic Gold Cluster Au₁₄₄(SR)₆₀

2009, *113,* 5035–5038 Published on Web 01/16/2009

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Olga Lopez-Acevedo,[†] Jaakko Akola,[†] Robert L. Whetten,[‡] Henrik Grönbeck,[§] and Hannu Häkkinen^{*,†,||}

Antiogra enbokatokt



Validate this prediction:

Measure X-ray diffraction data (in the form of an atomic pair distribution function (PDF))



The MD6441 structure: 144 gold atoms



Gold Au144





- Proper data validation illustrated theoretical limitation
- But our DFT colleagues told us the structural model also had to be incorrect: no low energy Au-thiol staples on the surface
- Better (correct?) model had a MD core and staples









Is there enough information for an ab-initio structure solution?

Example: C60

- 60 atoms => n(n-1)/2 = 1770 pair-vectors
- We know the lengths (not the directions) of ~18 unique distances
- We have an imperfect measure of the multiplicities of those distances
- We don't have any symmetry information to help us



Is the problem well conditioned or ill conditioned? Is there a unique solution?

Illustration of cluster buildup



ab-initio structure solution directly from PDF data











60 atoms

~64 atoms

C₆₀

Ultra-small CdSe NPs





Successology



Problem



Structure Solution







Complex Modeling Solution

- c = a + ib complex number mixes real and imaginary parts
- m = e + it complex modeling mixes experiment and theory in a coherent computational framework
- Billinge and Levin, Science 2007









Solving structure of nanoparticles and molecular solids



- Regular PDFgui fit gives peaks too sharp in high-r, too broad at low-r
- With Dragica Prill, Martin Schmidt and Juhas,
- Prill, Juhás, Schmidt and S.J.L.B., *J. Appl. Crystallogr.* 48, 171-178 (2015)

Refinement of molecular PDFs



Workaround using DSE + RSC

- Calculate molecule PDF using DSE (a)
- 2. Calculate crystal structure using RSC (b)
- Calculate molecule using DSE but with crystal structure ADPs (c)
- 4. Determine inter-molecular correlation from (b)-(c)
- 5. Add (a) and (d) to get full pattern (e)



- Result is excellent fit over whole range
- Dragica Prill, Pavol Juhás, Martin U.
 Schmidt and SJLB J.
 Appl. Crystallogr. 48, 171-178 (2015)





Update: Structure solution of molecular materials now possible



- pyobjcryst wraps functionality from ObjCryst++ (Favre-Nicolin and Cerny)
- Rigid body constraints and quaternions to describe spatial orientations of molecules
- Napthalene, P1, Z=2
- Blue is single crystal structure, red is PDF derived structure
- Dragica Prill, Pavol Juhás, S. J. L. Billinge and Martin U. Schmidt, Acta Crystallogr. A 72, 62-72 (2016)











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Spatially Resolved PDFs

 Anton Kovyakh, Soham Banerjee, Chia Hao Liu



High throughput allows spatially resolved tomographic imaging



- Experiments on ID15 at ESRF
- Pt/PtO nanoparticle catalyst on a γalumina support in a flow rig
- Have a fully refinable PDF in every pixel of the image
- Large particle size in a shell around the rim, small particle size and much lower density in the middle
- => Spatially resolved, time resolved nanostructure studies
- S. D. M. Jacques, Di Michiel, SJLB et al. *Nat. Commun.* 4, 2536 (2013)

Batteries



10,000 2D datasets per image, 30 mins per image ~10Tb/day Jensen, Corr, Di Michiel, SJLB et al., *J. Electrochem. Soc.* (2015)

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mPDF: PDF of short-range magnetic correlations



 Benjamin A. Frandsen, Xiaohao Yang and Simon J.L. Billinge, Acta Crystallogr. A 70, 3-11 (2014).







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MnO

Top: *Blue*: measured nPDF signal *Red* (top) calculated structural PDF Btm: *Blue*: difference between nPDFsignal and calculated structural PDF *Red*: calculated mPDF for AF MnO

Benjamin A. Frandsen, M. Brunelli, K. Page, Y. J. Uemura, Julie B. Staunton, SJLB, arXiv:1512.06270.

Frandsen, SJLB, Acta Crystallogr. A 71, 20325-334 (2015)

Summary



BROOKHAVEN





Summary

Many of society's toughest challenges require complex materials.

• Complex materials characterization present some of our toughest experimental and theoretical challenges

 In general, complex modeling solutions (combining multiple diverse information sources in a structure solution) will be needed to solve these problems



Underneath the Bragg Peaks

Structural Analysis of Complex Materials

SECOND EDITION



T. Egami S.J.L. Billinge

Powder Diffraction Theory and Practice

Ritherd by Bill Discontant and T. J. Millinger



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HTTP://t

RSCPublishing

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- MLNSC, ISIS, IPNS (and people therein)

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